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TS 1170.5

Background to Spectral Shape Recommendations  
from SRWG

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Tim Sullivan

University of Canterbury

# Overview

A number of spectral shape options were considered by the SRWG.

An overview of the procedure followed and key results are described in the following slides.

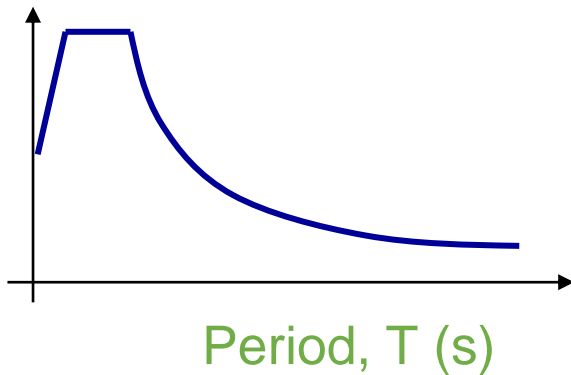
The final strength requirements are a result of the spectral shape, intensity and the design force expressions.

A later presentation will consider other factors, in addition to spectral shape, that were considered.

The likely impacts on the strength requirements will then be presented.

# NZS1170.5 Horizontal Elastic Response Spectrum

$$C(T) = C_h(T) \cdot Z \cdot R \cdot N(T, D)$$



where,  $Z$  = hazard factor  
 $R$  = return period factor.  
 $N(T, D)$  = near-fault factor  
 $C_h(T)$  = spectral shape factor

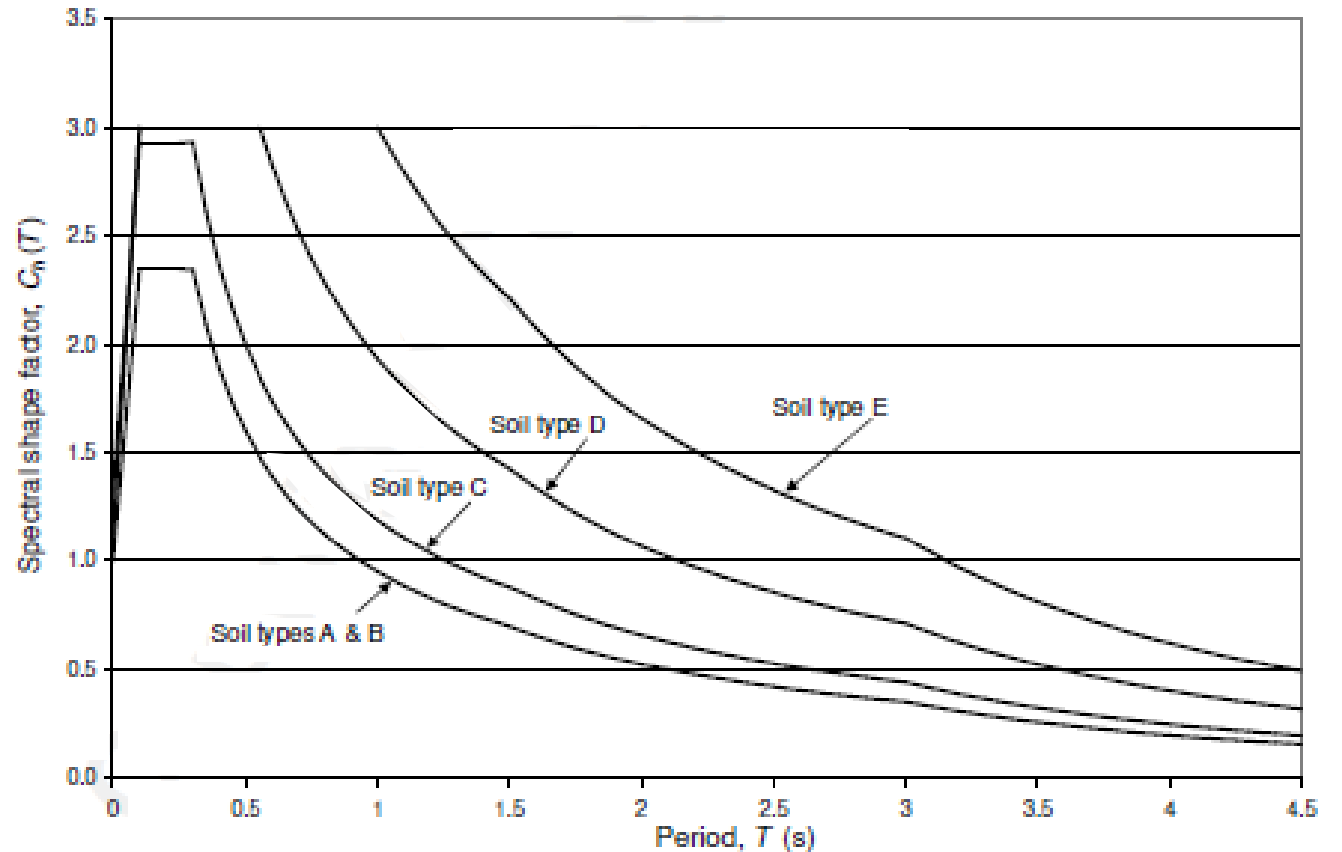


FIGURE 3.2 SPECTRAL SHAPE FACTOR,  $C_h(T)$  FOR MODAL ANALYSIS, NUMERICAL INTEGRATION TIME HISTORY ANALYSIS, VERTICAL LOADING AND PARTS

# Spectral shape approaches used internationally?

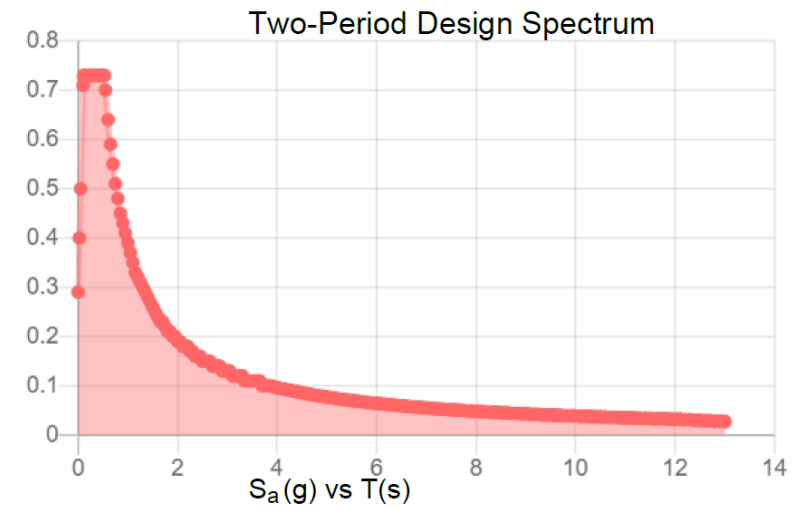
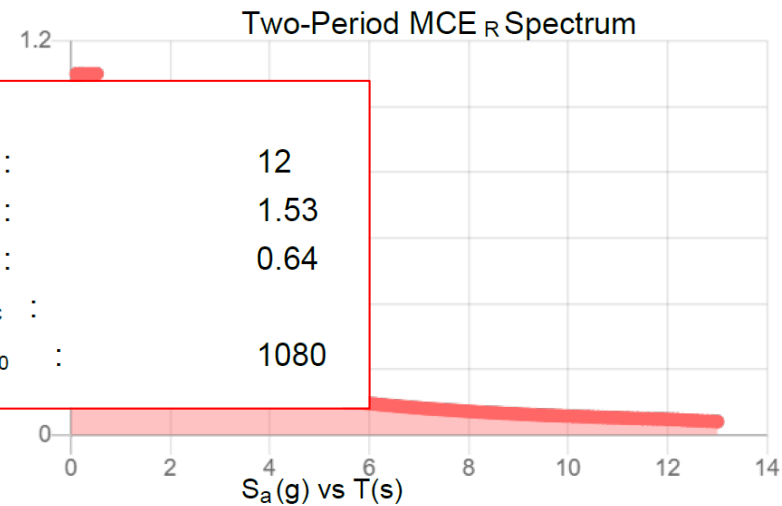
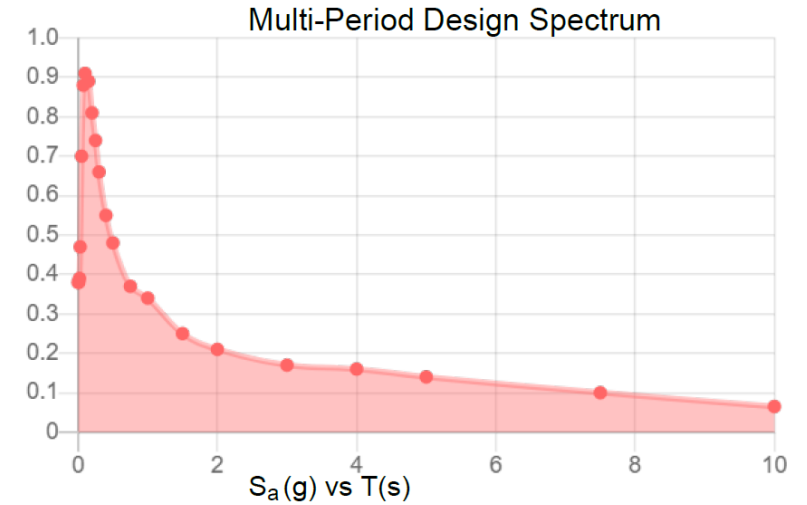
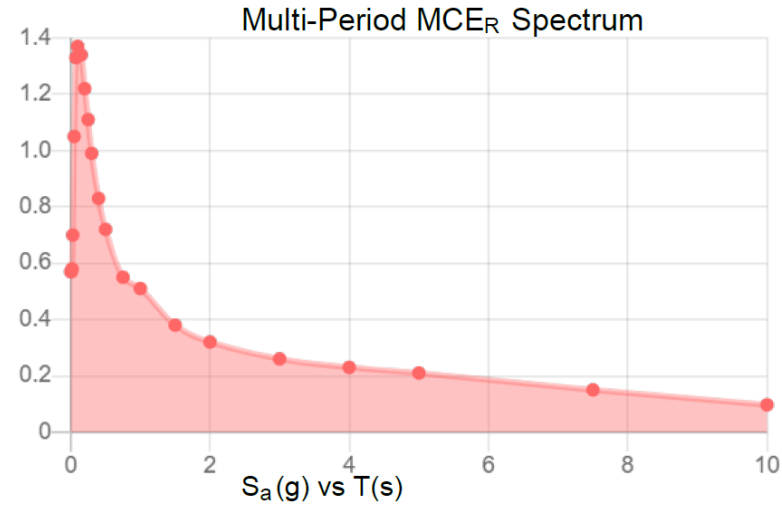
## US : ASCE7-22

Multi-point spectra.

See paper by Kircher & Rezaeian (2019)

Also:

<https://asce7hazardtool.online/>



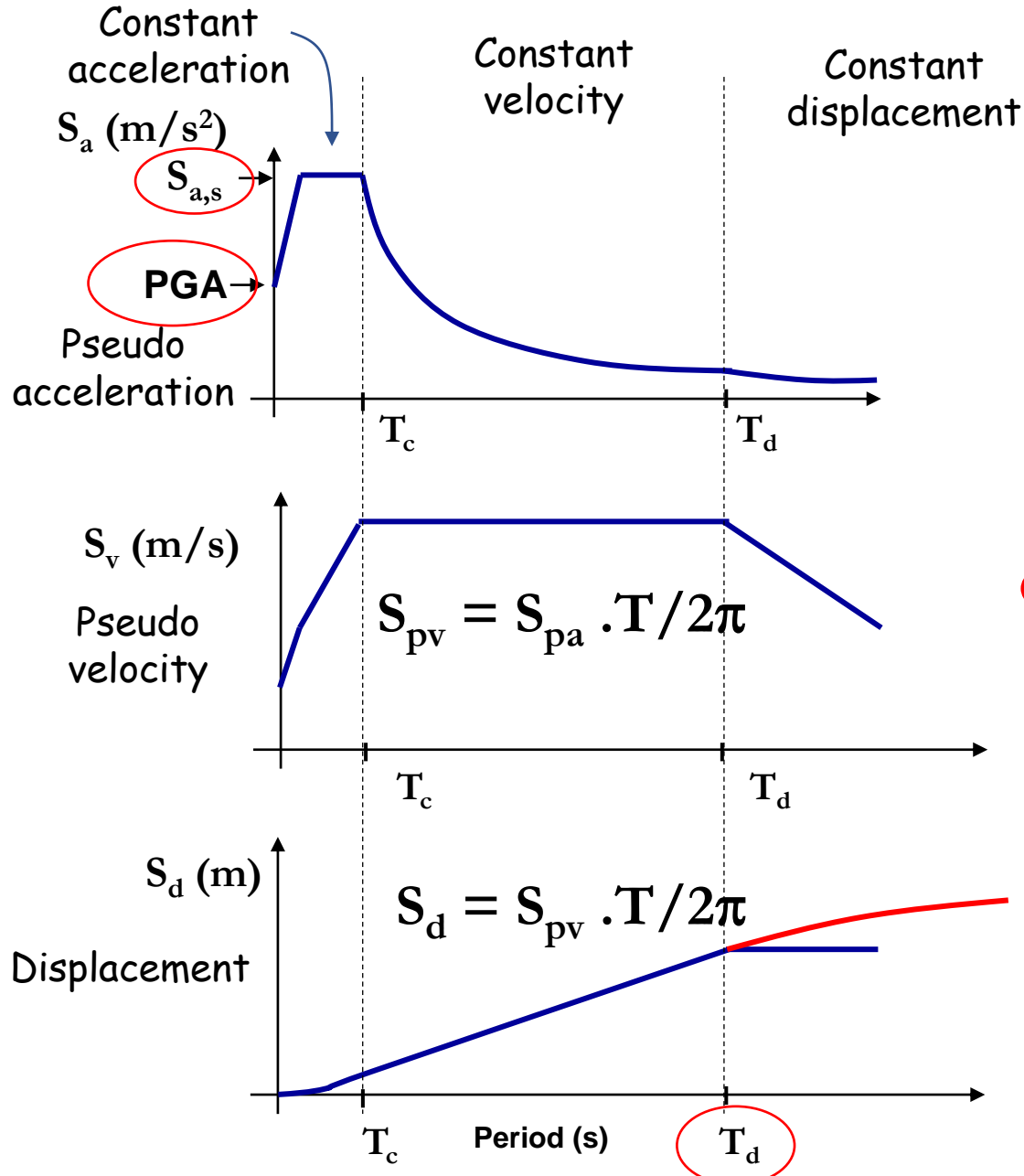
### Results:

$PGA_M$ :	0.46	$T_L$ :	12
$S_{MS}$ :	1.1	$S_S$ :	1.53
$S_{M1}$ :	0.58	$S_1$ :	0.64
$S_{DS}$ :	0.73	$S_{DC}$ :	
$S_{D1}$ :	0.39	$V_{S30}$ :	1080

# Options for spectral shape considered by SRWG

Spectral Shape Method	Description
<b>Method 0</b>	Keep spectral shapes currently in NZS1170.5
<b>Method 1</b>	New spectral shapes that vary only according to site-soil class
<b>Method 2</b>	New spectral shapes that vary according to site-soil class and two intensity ranges (low and high intensity)
<b>Method 3</b>	New design spectral shapes that vary (in a continuous fashion) according to site-soil class and intensity
<b>Method 4</b>	Fit design spectral shape directly to location specific UHS or Nominal Risk Spectra
<b>Method 5</b>	Use (multipoint) UHS or Nominal Risk Spectra directly without fitting any spectral shape functions.

# Options & equations for standardised design spectral shapes?



SRWG spectral shape equations:

$$S_a(T) = PGA \quad \text{for } T = 0s \quad (7)$$

$$S_a(T) = S_{a,s} \quad \text{for } 0.1s < T < T_c \quad (8)$$

$$S_a(T) = S_{a,s} \frac{T_c}{T} \quad \text{for } T_c < T < T_d \quad (9)$$

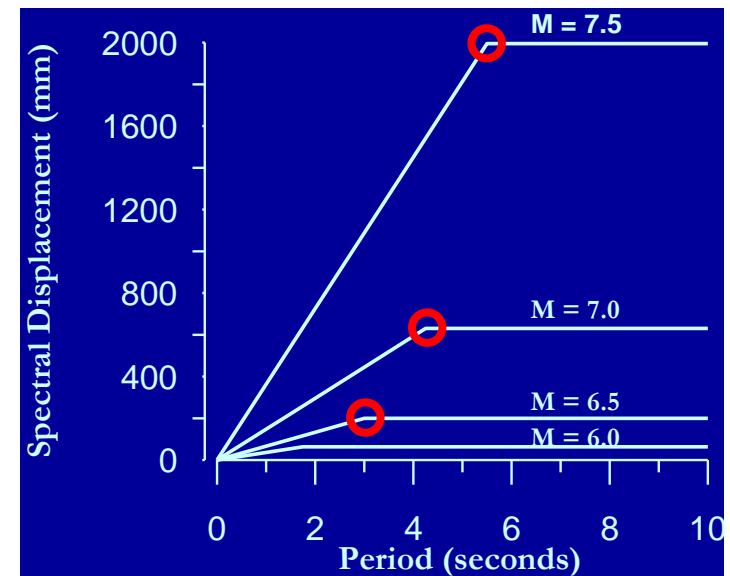
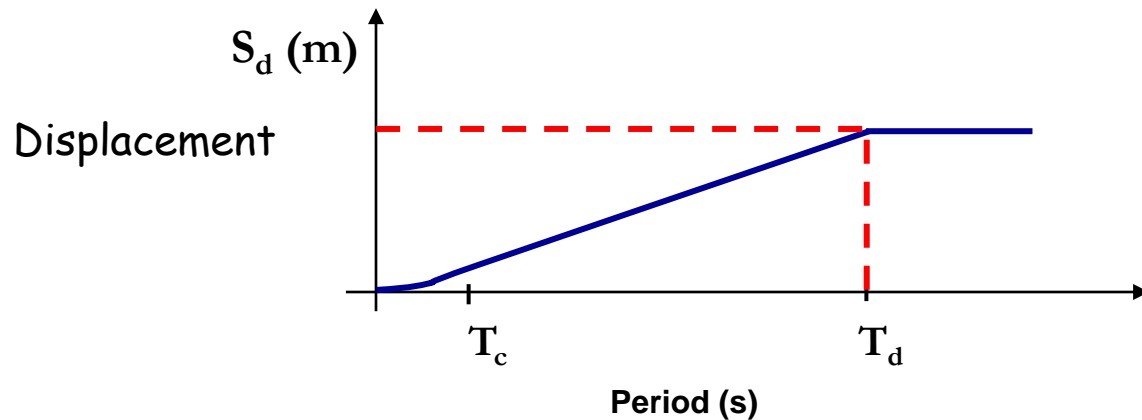
$$S_a(T) = S_{a,s} \frac{T_c}{T} \left(\frac{T_d}{T}\right)^{0.5} \quad \text{for } T_d < T \quad (10)$$

Why the new expression for  $S_a(T)$  at long periods,  $T > T_d$  ?

# Spectral shape at long periods?

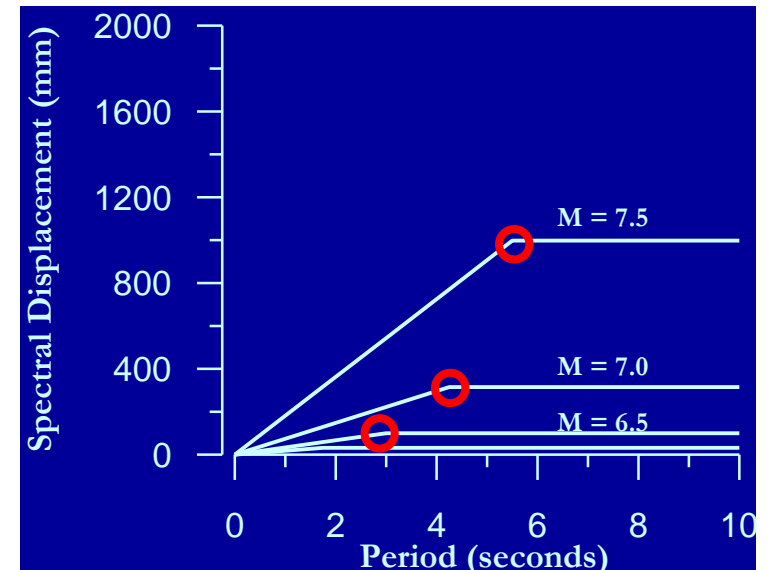
Faccioli et al. (2004) examined shape of spectra at long periods and noted:

- At very long periods (e.g.  $T > 10\text{s}$ ), the spectral displacement demand corresponds to the peak ground displacement.
- The period,  $T_d$ , at which peak spectral displacement demand develops was found to be a function of earthquake magnitude,  $M$ .
- The peak value of the displacement depends on both the EQ magnitude and fault distance,  $r$ .



## 5% Damped Spectra at $r = 10\text{km}$

Figures from Priestley et al. (2007)



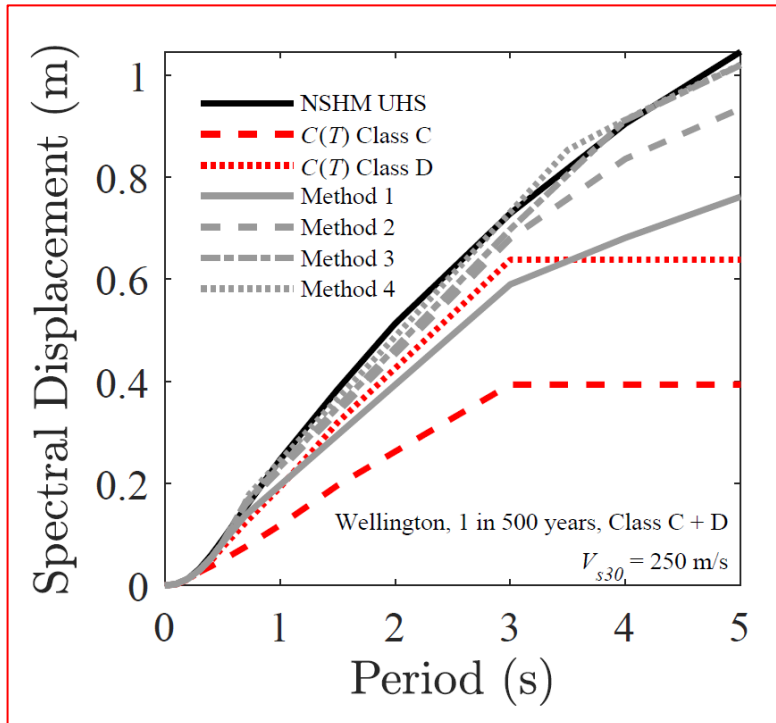
## 5% Damped spectra at $r = 20\text{ km}$

# Relevance for shape of UHS at long periods?

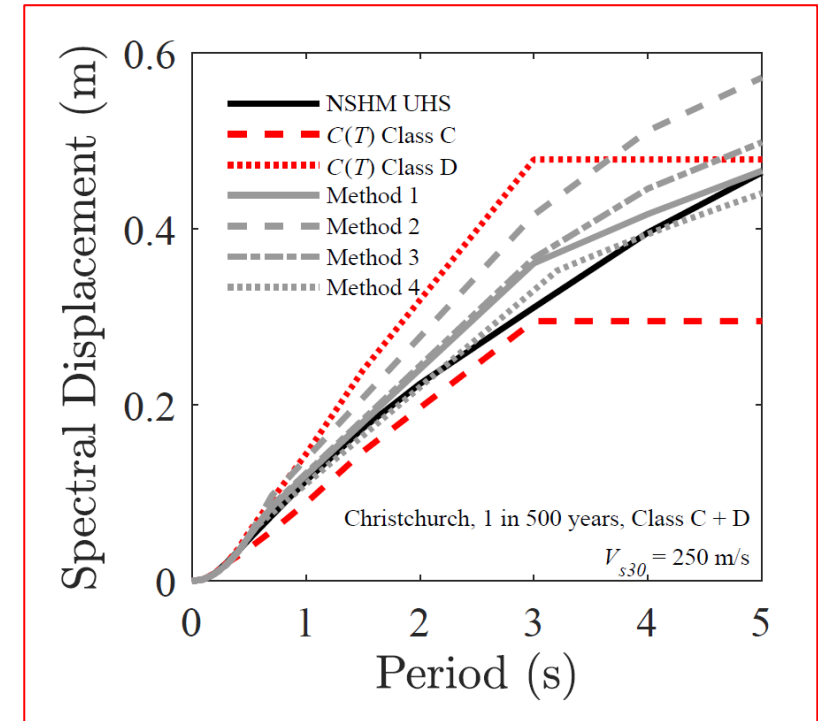
Uniform hazard spectra (UHS) demands are affected by a wide range of possible earthquake magnitudes,  $M$ , and distances,  $r$ .

→ hence, UHS don't typically exhibit a clear plateau in spectral displacement demands, even though demands at long periods do tend to flatten.

Wellington  
 $T_R = 500\text{yrs}$



Christchurch  
 $T_R = 500\text{yrs}$



The new equation for long period demands captures this flattening better than old.



# Setting elastic design spectrum considering UHS?

In addition to shape functions, need a procedure for fitting a design spectral shape to mean UHS (or notional risk spectrum).

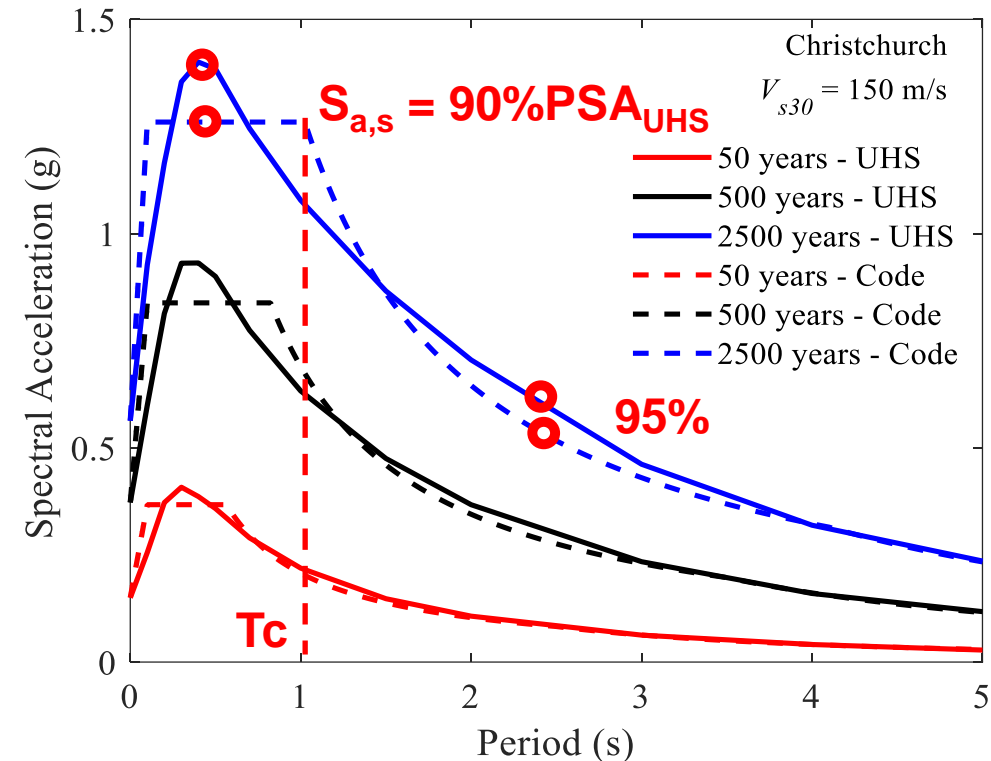
SRWG procedure:

- The PGA is taken directly from the UHS data.
- The short period acceleration demand,  $S_{a,s}$ , is taken as 90% the peak spectral acceleration demand.
- The spectral acceleration corner period,  $T_c$ , is set by the following equation:

$$T_c = \frac{2\pi PSV}{S_{a,s}} \quad (11)$$

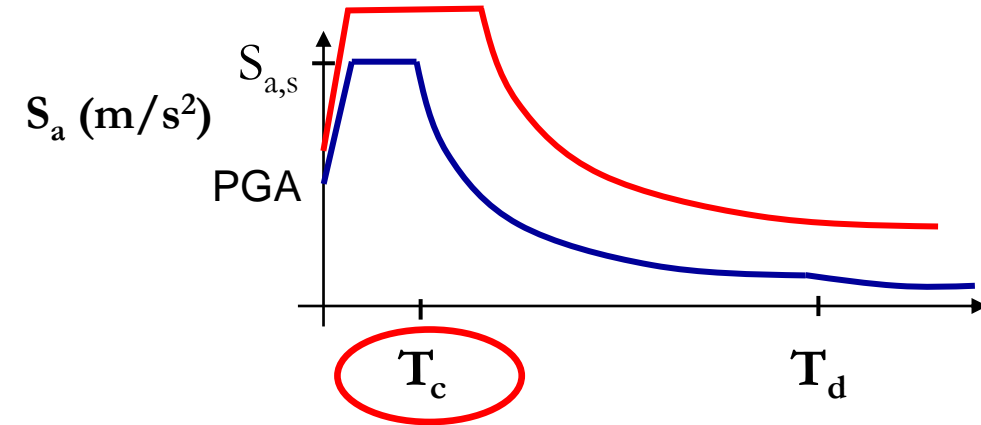
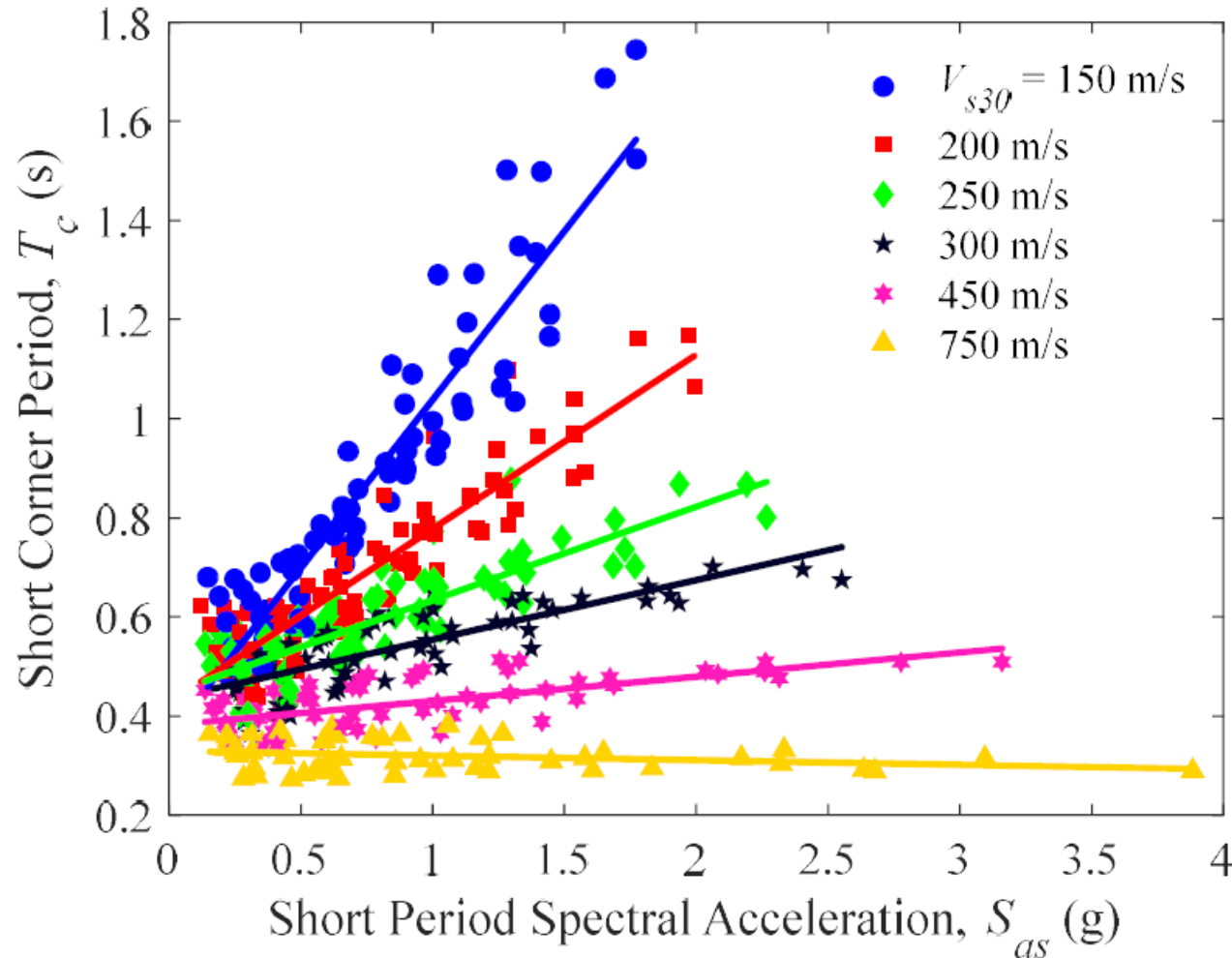
where PSV is the peak spectral velocity that has been taken equal to 95% the actual PSV from the UHS (in order to achieve a good fit with spectral demands across the medium period range).

- The spectral displacement corner period,  $T_d$ , was initially obtained via least-squares regression to minimise the difference between the UHS and design spectrum values for spectral velocity (between  $T_c$  and  $T_{max}$ ) but then set to 3s as discussed later.



# How much does the corner period, $T_c$ , vary with intensity?

Values of  $T_c$  obtained for 12 cities, six Vs30 values and all return periods:



**$T_c$  seen to be a function of earthquake shaking intensity, as well as  $V_{s,30}$  (site class)**

Figure 9: Variation of the short corner period as a function of short period spectral acceleration.

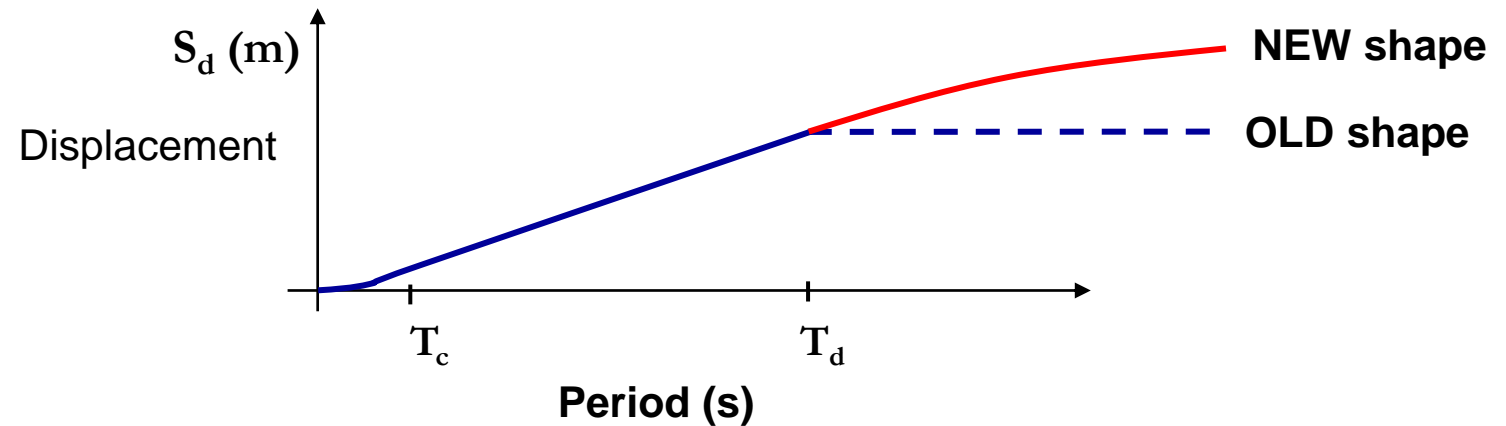
# But what about the spectral velocity plateau corner period, $T_d$ ?

A desire was expressed to seek a single value of  $T_d$  if possible, for simplicity.

The new functional form for demands beyond  $T_d$  implies that accuracy of UHS fit is less sensitive to the value of  $T_d$  adopted.

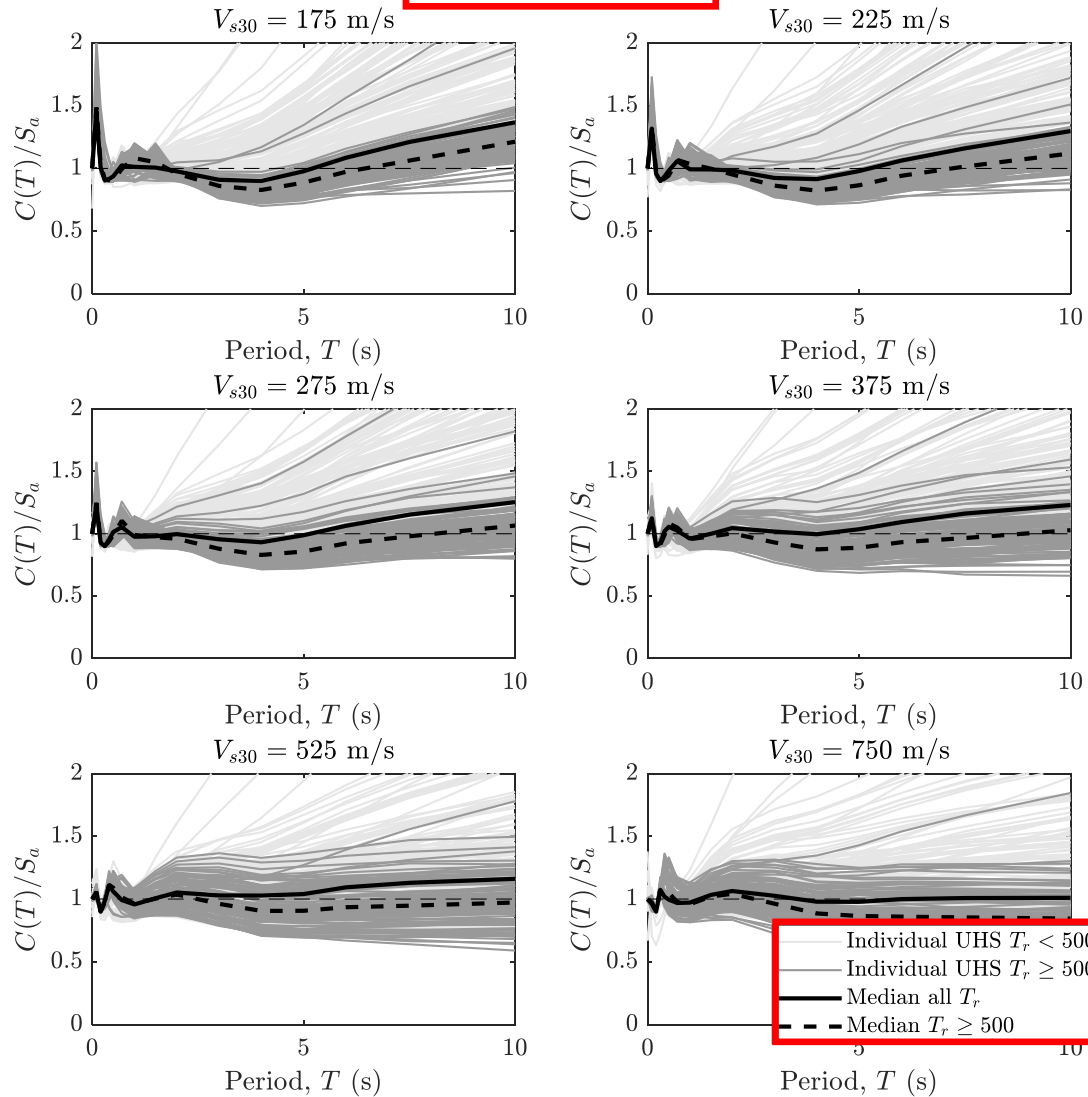
The following options for values of  $T_d$  values were trialled:

- $T_d = 2.0s$
- $T_d = 2.5s$
- $T_d = 3.0s$
- $T_d =$  fitted site-by-site

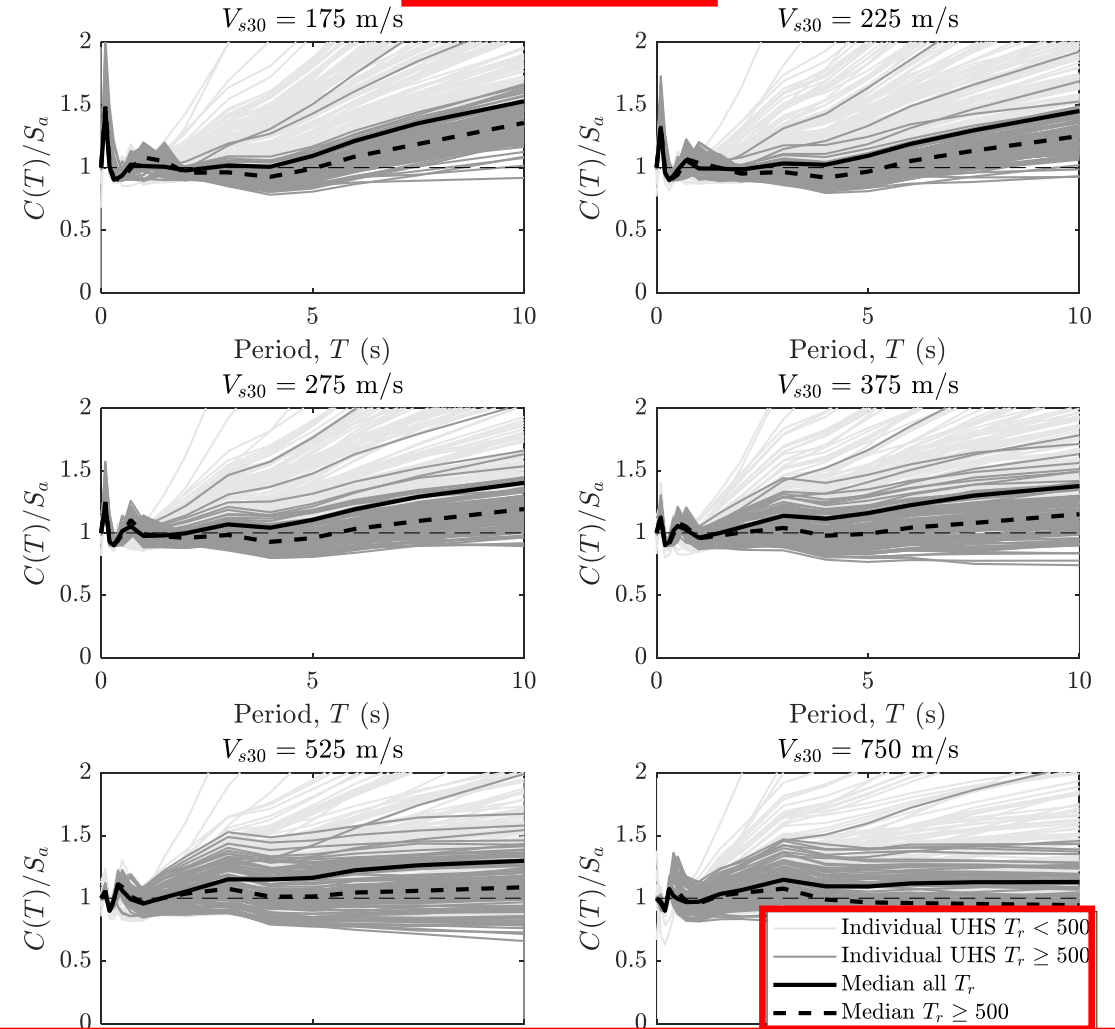


# Ratio of design spectrum $S_a$ to UHS value of $S_a$

$$T_d = 2 \text{ s}$$



$$T_d = 2.5 \text{ s}$$



## Things to note:

- Values  $> 1.0$  indicate conservative design requirement

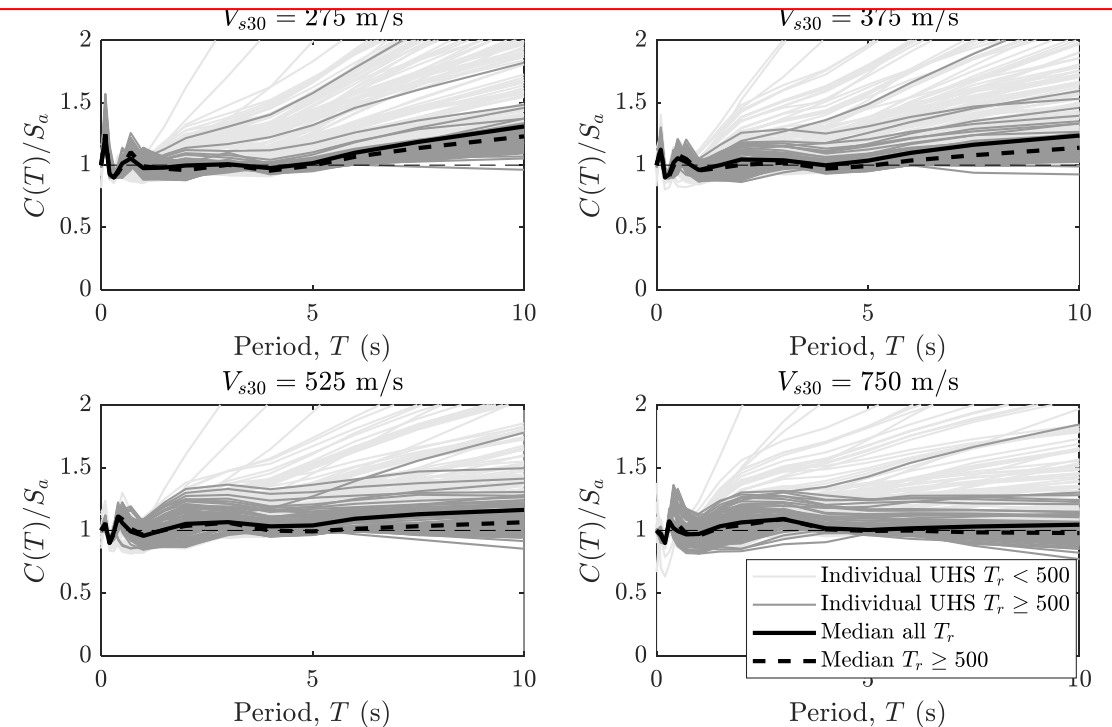
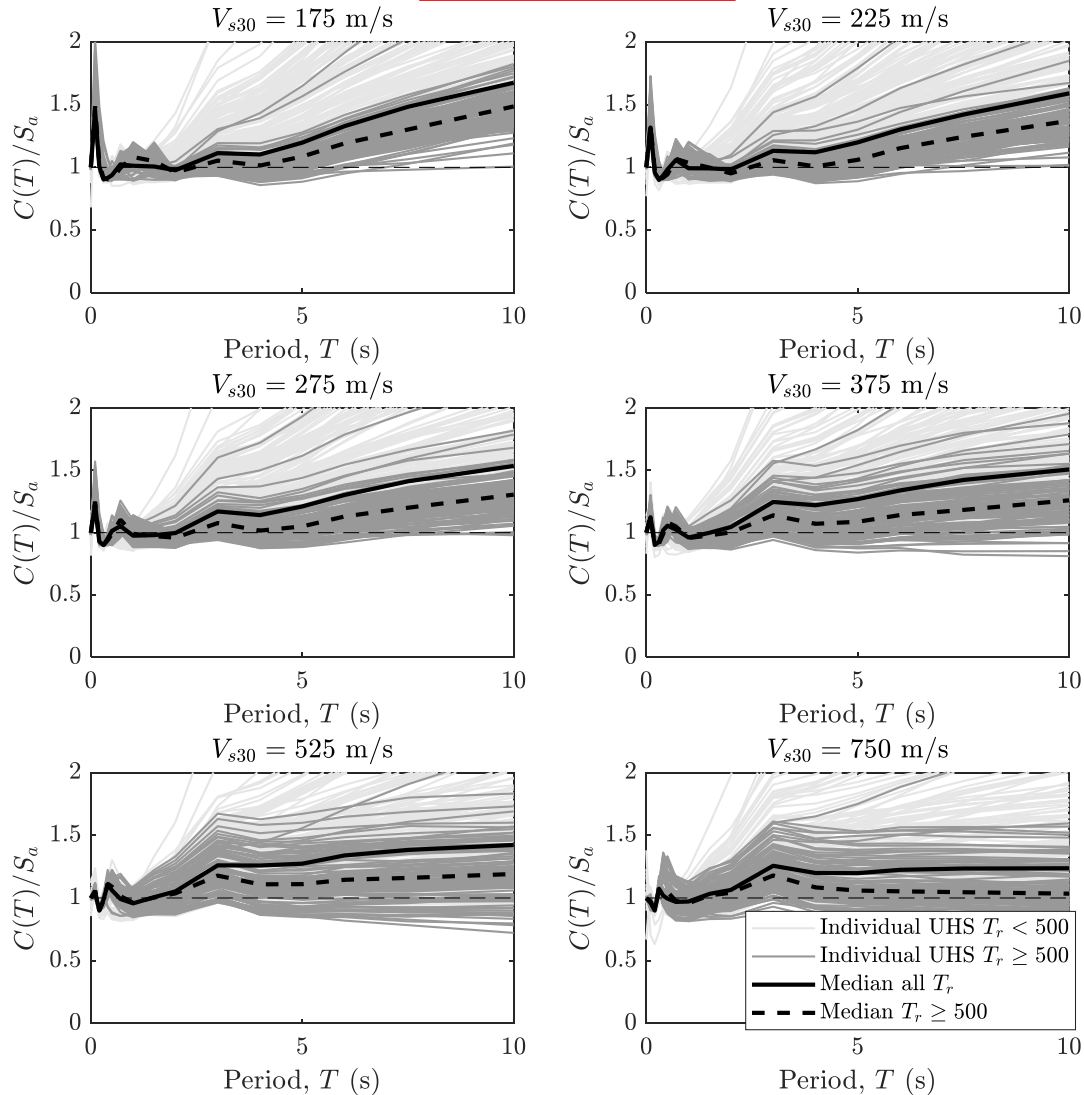
# Ratio of design spectrum $S_a$ to UHS value of $S_a$

$T_d = 3 \text{ s}$

$T_d$  Fitted

The SRWG agreed to adopt  $T_d = 3\text{s}$  noting:

- Values  $> 1.0$  indicate conservative design requirement
- Use of  $T_d = 3.0\text{s}$  is slightly conservative for most locations at ULS, out to  $T = 5.0 - 6.0\text{s}$
- Use of  $T_d = 3.0\text{s}$  is clearly conservative for SLS (small return periods).



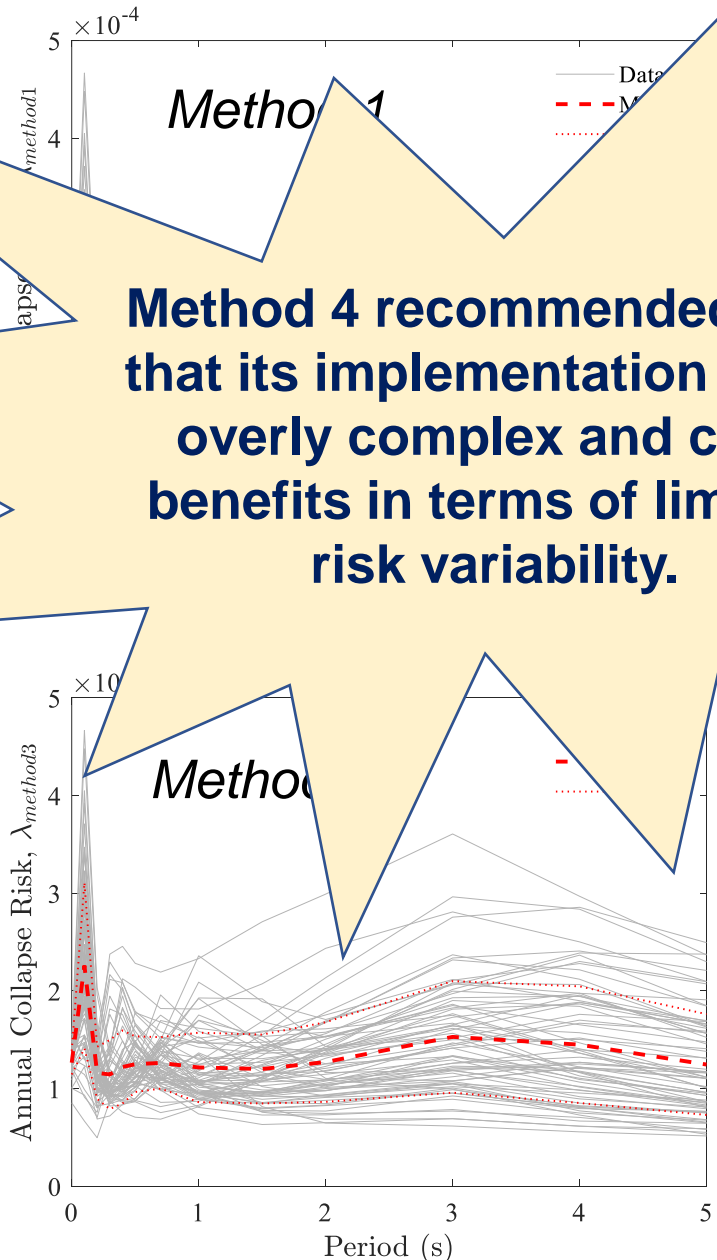
# Evaluation of spectral shape options

Consider:

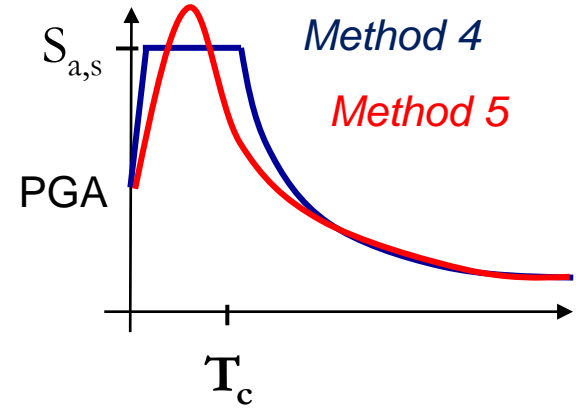
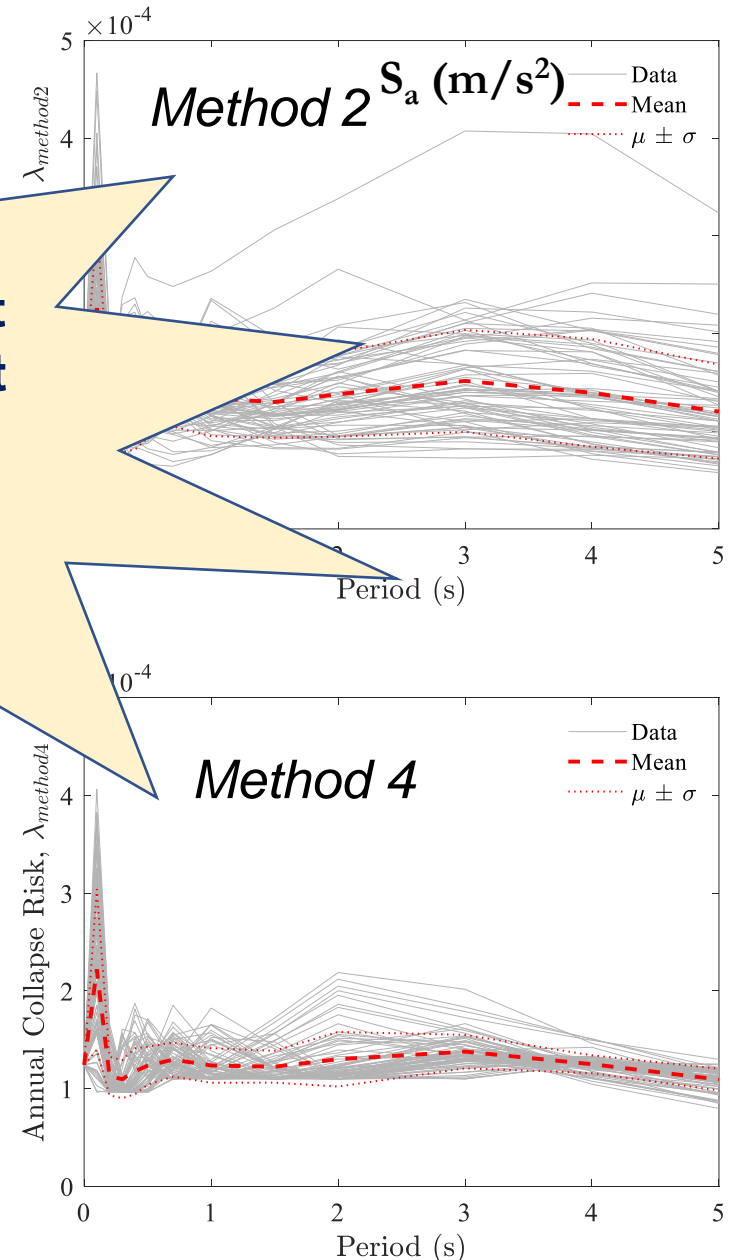
- How option could be implemented in a code
- Implications for strength requirements
- Implications for risk variability

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# Approximate variability in risk due to spectral shape choices?



**Method 4 recommended. Felt that its implementation is not overly complex and clear benefits in terms of limiting risk variability.**



A benefit of Method 4 over Method 5 (smooth UHS) is that simplified spectral shape is less sensitive to period estimates in short period range.

# Method 4 – using fitted UHS defined as a function of location, intensity (annual prob of exceedance) and site class

Implementation thought to be best via an on-line tool, similar to US/Italy etc. approaches.

Also identified that a fit spectrum could be defined according to each site class and return period with only three tabulated variables: PGA,  $S_{as}$  and  $T_c$

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TABLE 3.4(e) part 5: Site demand parameters for an annual probability of exceedance of 1/500

Location	M	D	Site Class I			Site Class II			Site Class III			Site Class IV			Site Class V			Site Class VI		
			PGA	$S_{as}$	$T_c$	PGA	$S_{as}$	$T_c$	PGA	$S_{as}$	$T_c$	PGA	$S_{as}$	$T_c$	PGA	$S_{as}$	$T_c$	PGA	$S_{as}$	$T_c$
Masterton	7.9	6	1.0	2.21	0.3	1.05	2.19	0.4	1.03	2.03	0.5	0.95	1.82	0.6	0.89	1.68	0.8	0.8	1.53	1.1
Paekakariki	7.8	16	0.8	1.78	0.3	0.86	1.81	0.4	0.86	1.74	0.5	0.82	1.62	0.6	0.78	1.54	0.8	0.72	1.44	1.0
Carterton	7.9	4	1.0	2.2	0.3	1.04	2.18	0.4	1.02	2.03	0.5	0.95	1.82	0.7	0.88	1.69	0.8	0.8	1.54	1.1
Greytown	7.9	4	0.96	2.12	0.3	1.01	2.12	0.4	1.0	1.98	0.5	0.93	1.79	0.6	0.87	1.67	0.8	0.79	1.53	1.1
Porirua	7.8	6	0.82	1.82	0.3	0.88	1.86	0.4	0.88	1.78	0.5	0.84	1.66	0.6	0.79	1.56	0.8	0.73	1.46	1.1
Featherston	7.9	0	0.97	2.14	0.3	1.02	2.14	0.4	1.01	2.0	0.5	0.94	1.81	0.7	0.87	1.68	0.8	0.79	1.54	1.1
Motueka	7.4	>20	0.34	0.74	0.3	0.38	0.82	0.4	0.41	0.88	0.5	0.42	0.92	0.6	0.43	0.95	0.7	0.42	0.98	0.8
Upper Hutt	7.8	0	0.9	1.98	0.3	0.95	2.01	0.4	0.95	1.9	0.5	0.89	1.74	0.7	0.83	1.63	0.8	0.76	1.51	1.1
Lower Hutt	7.8	0	0.86	1.9	0.3	0.92	1.93	0.4	0.92	1.85	0.5	0.87	1.7	0.7	0.81	1.6	0.8	0.74	1.49	1.1
Martinborough	7.9	16	0.94	2.07	0.3	0.99	2.06	0.4	0.98	1.93	0.5	0.91	1.75	0.6	0.85	1.63	0.8	0.78	1.5	1.1

Table above are for a constant value of  $T_d = 3.0s$

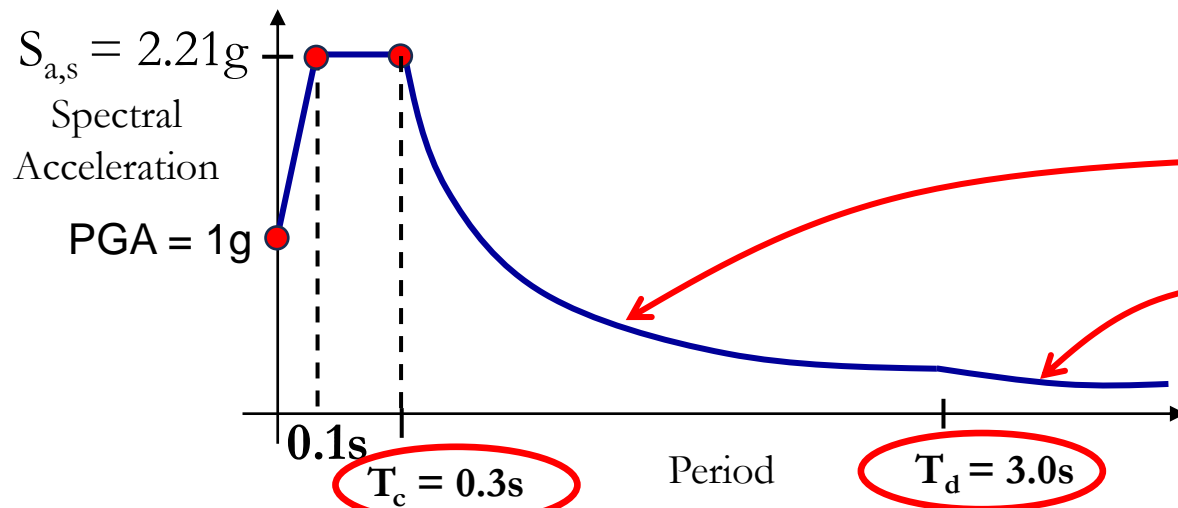


# So how can we get spectral shape from TS1170.5?

Need: Location, Site class & Annual Probability of Exceedance.

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			PGA	S <sub>a,s</sub>	T <sub>c</sub>	PGA	S <sub>a,s</sub>	T <sub>c</sub>	PGA	S <sub>a,s</sub>	T <sub>c</sub>	PGA	S <sub>a,s</sub>	T <sub>c</sub>	PGA	S <sub>a,s</sub>	T <sub>c</sub>	PGA	S <sub>a,s</sub>	T <sub>c</sub>
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$$S_a(T) = PGA \quad \text{for } T = 0s$$

$$S_a(T) = S_{a,s} \quad \text{for } 0.1s < T < T_c$$

$$S_a(T) = S_{a,s} \frac{T_c}{T} \quad \text{for } T_c < T < T_d$$

$$S_a(T) = S_{a,s} \frac{T_c}{T} \left(\frac{T_d}{T}\right)^{0.5} \quad \text{for } T_d < T$$

Impact of new design spectra on  
design strength requirements?

# Design strength expression

$$V_e = C_d(T_1)W_t$$

$$C_d(T) = \frac{C(T)S_p}{k_\mu}$$

$$C(T) = S_a(T)N(T,D)$$

where

$S_a(T)$  = the spectral acceleration in units of g determined from Clause 3.1.2

$N(T,D)$  = the near-fault factor determined from Clause 3.1.4

# Near fault factor, N(T,D)?

The NSHM data does not explicitly allow for near-fault effects and directivity.

From a total risk perspective it is considered that the current approach for dealing with near fault effects is conservative (Weatherill, 2022). However, a suitable alternative has not been identified.

The SRWG recommends that near fault factors continue to be set as in NZS1170.5 (2004), except using updated distances D, and that a review of the provisions for near-fault and directivity effects be made in Phase II of the SRWG programme.

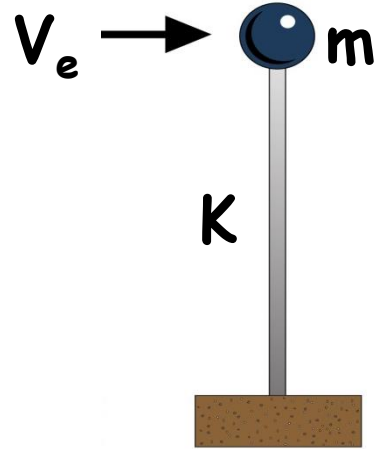
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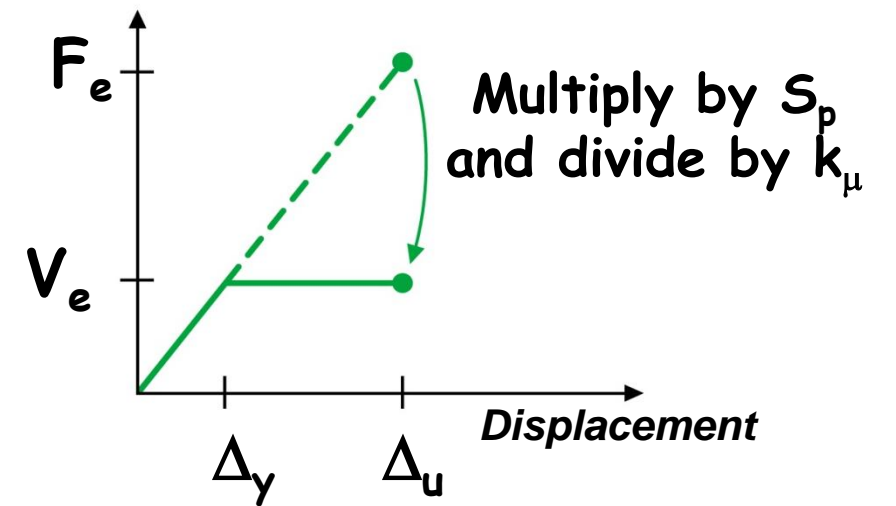
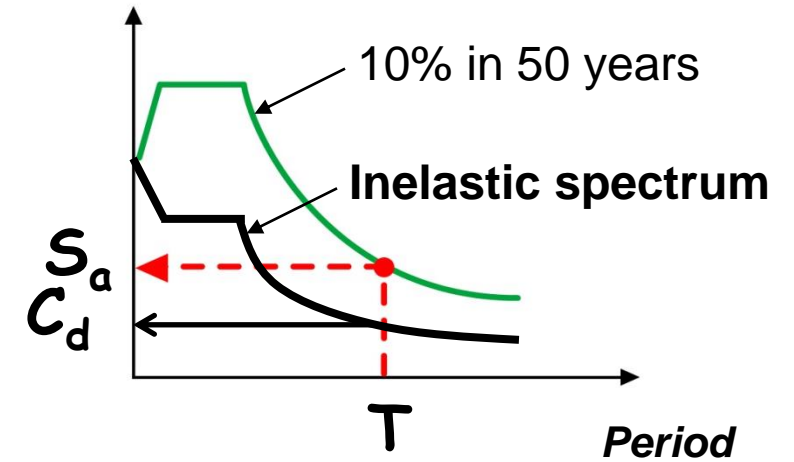
# Allowing for inelastic deformation capacity via $k_\mu$ factor?

$$V_e = W_t \cdot C_d$$

$$V_e = W_t \cdot C_d$$



$$C_d(T) = \frac{C(T)S_p}{k_\mu}$$



# Existing expressions for $k_\mu$ factor in NZS 1170.5 (2004)?

$k_\mu$  = inelastic spectrum scaling factor

for soil class A-D

$$\begin{aligned} k_\mu &= \mu && \text{for } T \geq 0.7\text{s} \\ &= (\mu-1)T/0.7 + 1 && \text{for } T < 0.7\text{s} \end{aligned}$$

for soil class E

$$\begin{aligned} k_\mu &= \mu && \text{for } T \geq 1\text{s or } \mu < 1.5 \\ &= (\mu-1.5)T + 1.5 && \text{for } T < 1\text{s and } \mu \geq 1.5 \end{aligned}$$

Note: T shall not be taken less than 0.4s for the purpose of calculating  $k_\mu$

Could a larger  $k_\mu$  factor be justified for short periods?

The SRWG generally felt it was not feasible to re-examine  $k_\mu$  factors and structural analysis provisions in this first set of revisions.

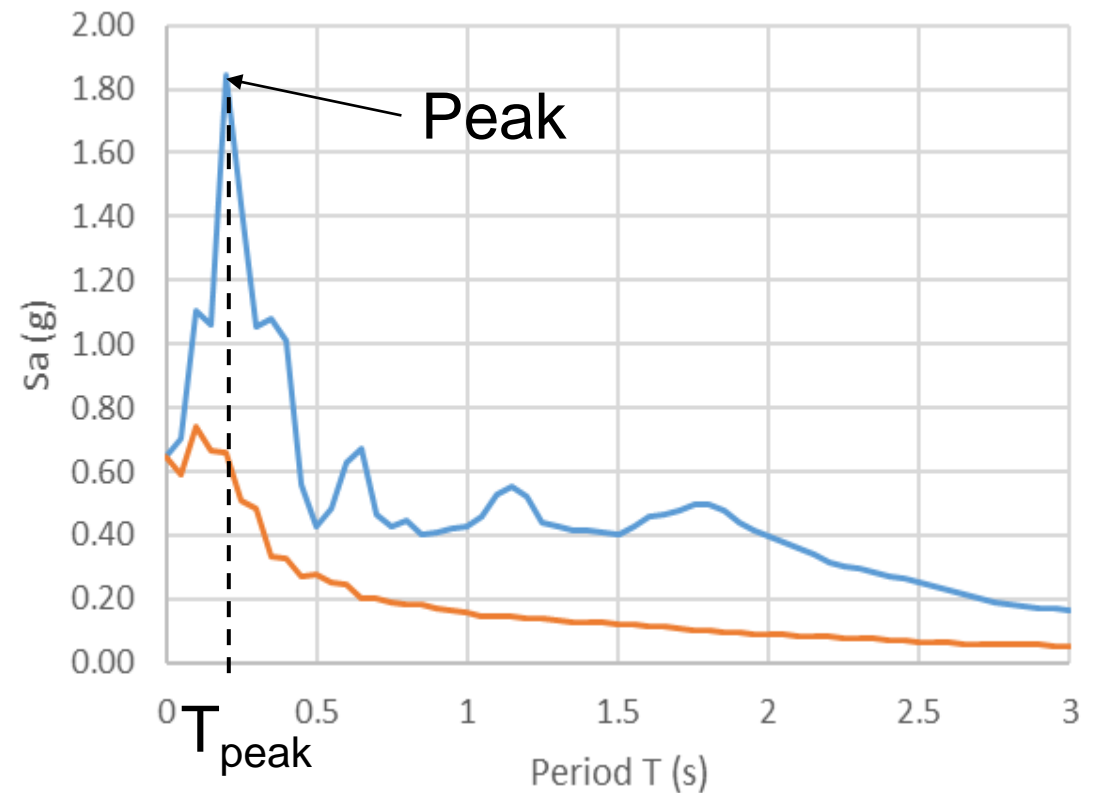
However, the SRWG were also concerned that demands on short-period buildings resulting from the new NSHM could be unreasonably high.

# Could a larger $k_\mu$ factor be justified at short periods?

Beyond what period of vibration could the equal-displacement rule be applied?

It is currently applied for  $T > 0.7\text{s}$  for most site classes in NZS 1170.5 (2004)

→ Consider apparent  $k_\mu$  factors from inelastic spectra plotting  $T$  relative to a peak period,  $T_{\text{peak}}$ .

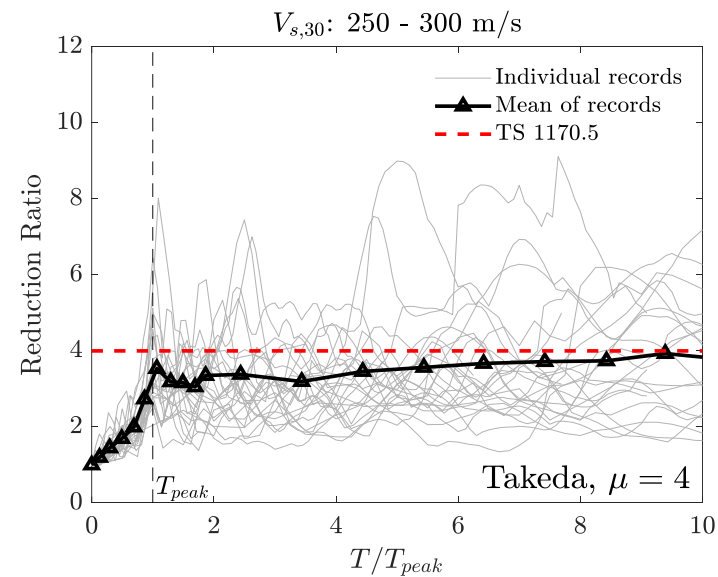
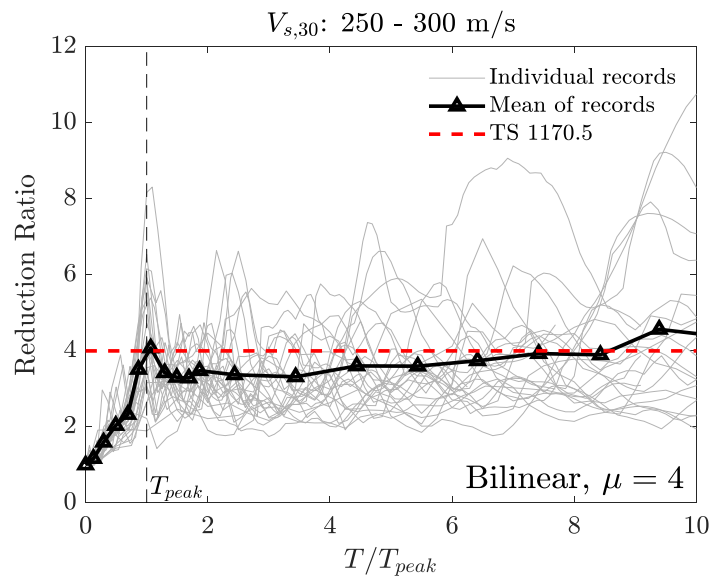
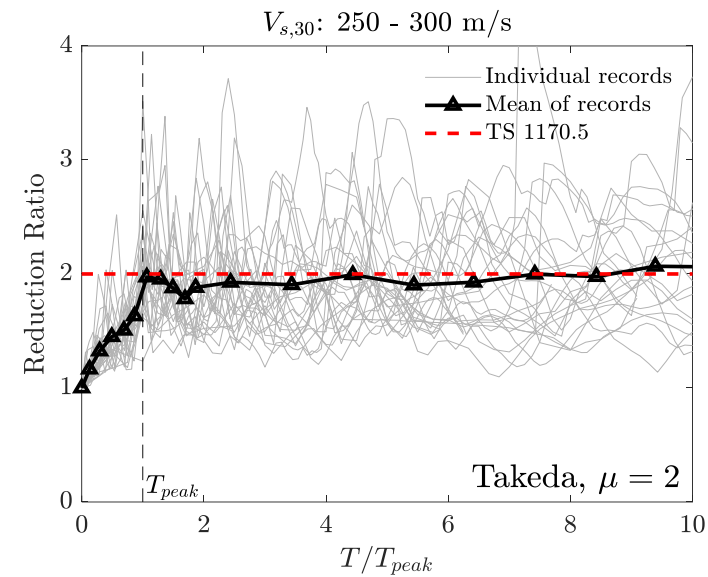
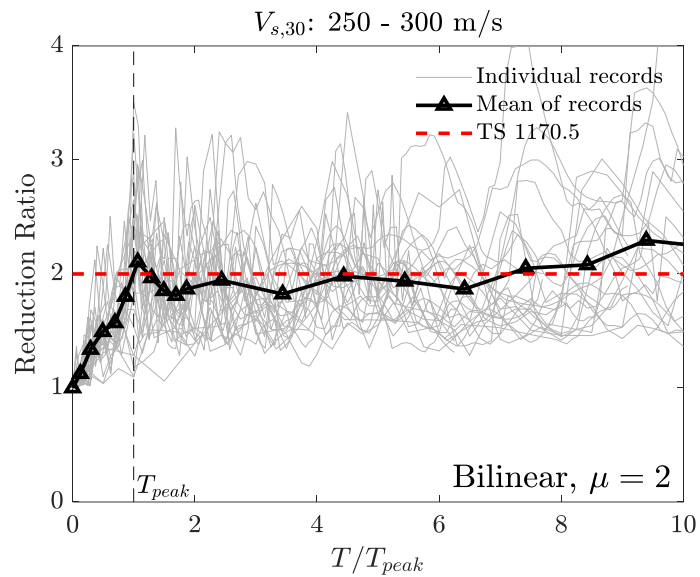


# Investigation of demands using suite of records

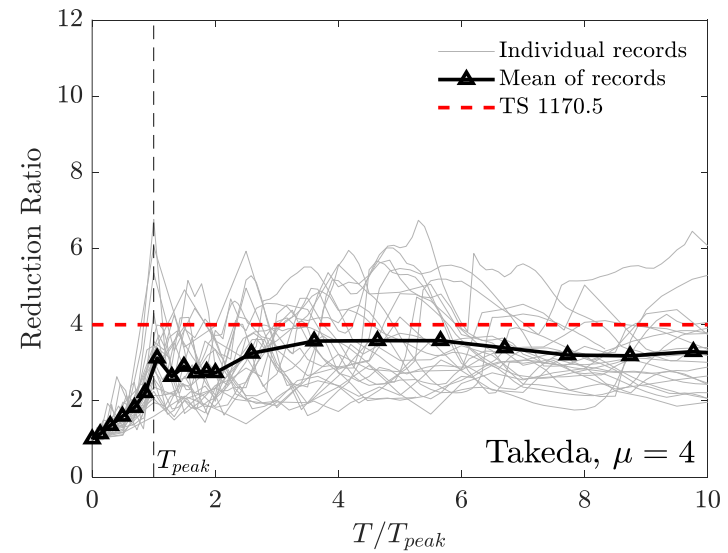
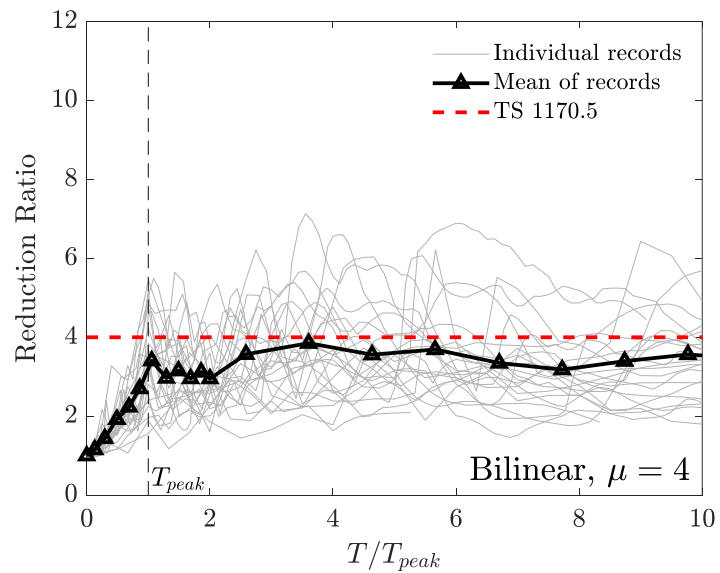
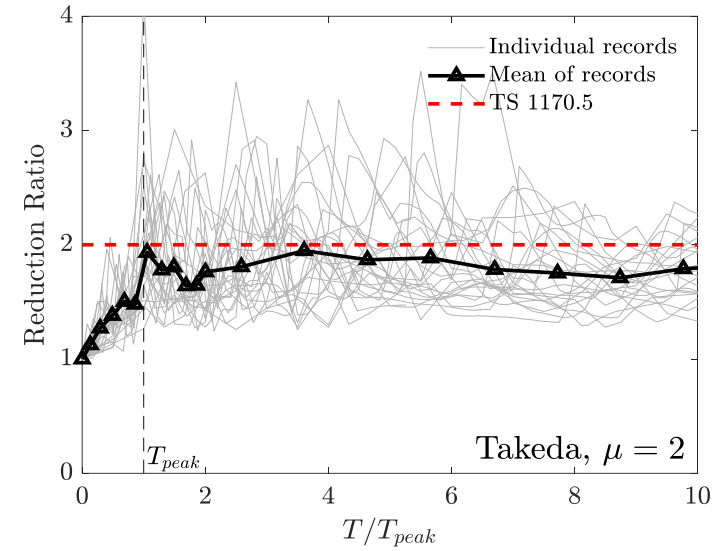
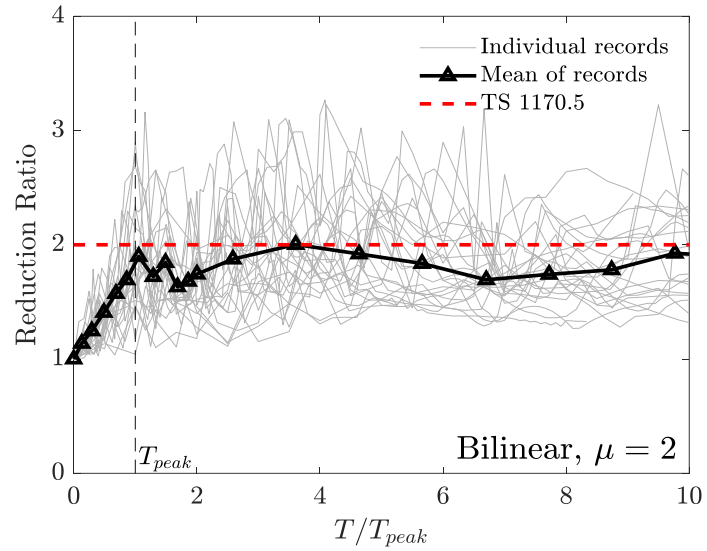
- Suite of records from PEER NGA-West2 Database
- $M_w > 5.5$
- Pulse-like records excluded
- Inelastic spectra developed using INSPECT (Carr) with following assumptions:
  - Bi-linear and Takeda hysteretic models with post-yield stiffness ratio,  $r = 0.05$
  - Takeda parameters: Emori Schonbrich reloading with  $\alpha = 0.5$  and  $\beta = 0.0$
  - Secant proportional damping ratio 5%.



# Soft soil sites: $V_{s,30} = 250 \text{ m/s} - 300 \text{ m/s}$



# Rock sites: $V_{s30} = 700 \text{ m/s} - 2000 \text{ m/s}$





# New expressions for $k_\mu$ factor?

Initial suggestion:

$$\begin{aligned} k_\mu &= \mu && \text{for } T \geq T_c/2 \\ &= (\mu-1)T/0.7 + 1 && \text{for } T < T_c/2 \end{aligned}$$

$$k_\mu = \mu$$

Because the value of  $T_{peak}$  is low and because members of the SRWG feel that there is some anecdotal evidence that short period buildings are already very resilient, the SRWG is recommending  $k_\mu = \mu$  for all periods of vibration.

A recent study in US (FEMA P-2139-1, 2020) also found that short-period buildings are not as prone to collapse as traditional design provisions might suggest.

Key reasons:

- Design ductility values and associated displacement capacities for timber-framed buildings, steel CBF buildings and reinforced masonry buildings are too conservative for short period buildings.
- A small lateral deformation of foundations (not accounted for in structural analyses) could significantly increase the period & total deformation capacity.

## Design strength implications?

$$V_e = C_d(T_1)W_t$$

The following slides present the resulting design coefficients,  $C_d(T)$ , for some of the main cities around New Zealand.

$$C_d(T) = \frac{C(T)S_p}{k_\mu}$$

Results are for  $T_r = 500$  years (ULS).

Results show elastic demands and demands for  $\mu = 4.0$ .

Design coefficients are compared with the existing NZS 1170.5 (2004) provisions (but with uncertainty in equivalence of site classes)

# Soil Classification Compatibility for Inelastic Spectra Comparison

1. NZS1170.5 site classes encompass a wide range of  $V_s(30)$  values (e.g., Site Class C in WEL has  $V_s(30)=200-500\text{m/s}$ )
2. For a given  $V_s(30)$  value, several different site classes could be specified in NZS1170.5 (e.g.,  $V_s(30)=250\text{m/s}$  can be Class C, D or even E)
3. The range of  $V_s(30)$  values corresponding to a given site class in NZS1170.5 is region-(location)-dependent (e.g., typically for Site Class D:  $V_s(30)=175-225\text{ m/s}$  in CHC; but is  $V_s(30)=200-350\text{m/s}$  in WEL).

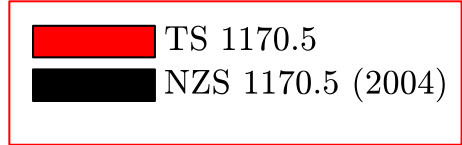
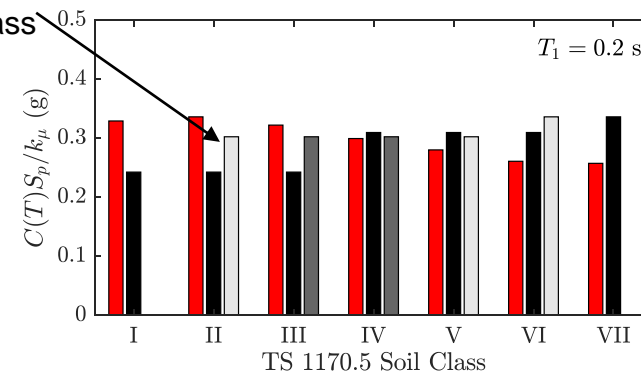
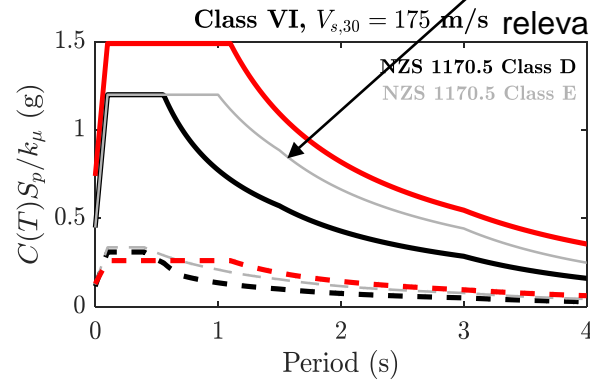
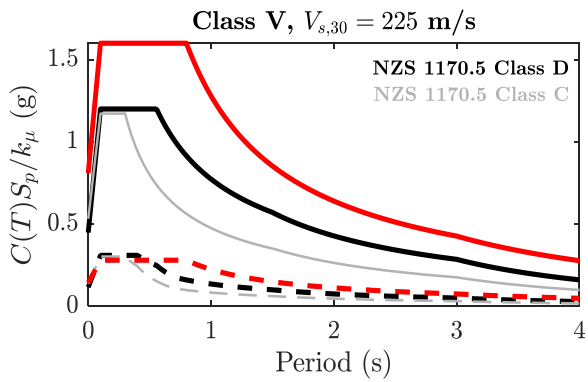
Given the above (courtesy of Misko), inelastic spectra comparisons are made considering the soil classification relationships shown in the table below:

**(a) Site classes in black are equally appropriate**

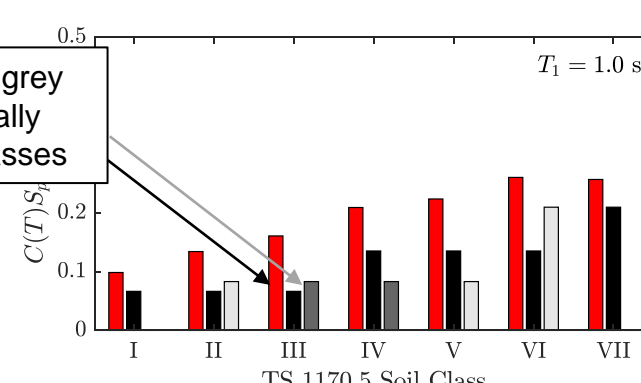
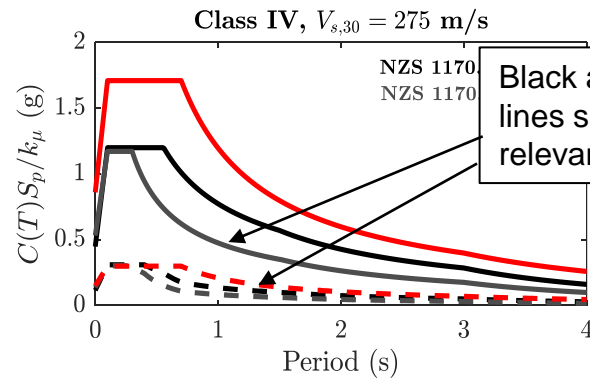
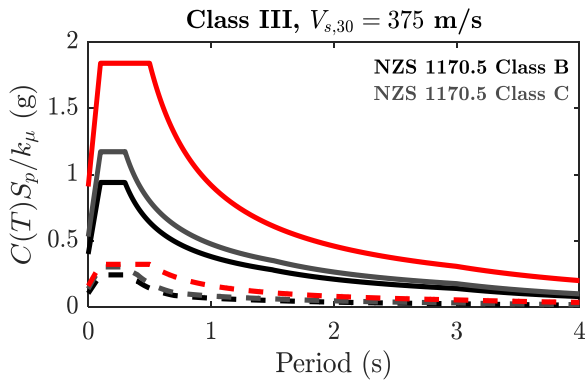
**(b) Site classes in red are less likely in relative terms but still relevant**

$V_{s30}$ (m/s)	TS 1170.5 site class	NZS 1170.5 (2004)	
150	VII	E	
175	VI	D	E
225	V	D	C
275	IV	D	C
375	III	B	C
525	II	B	C
750	I	A	

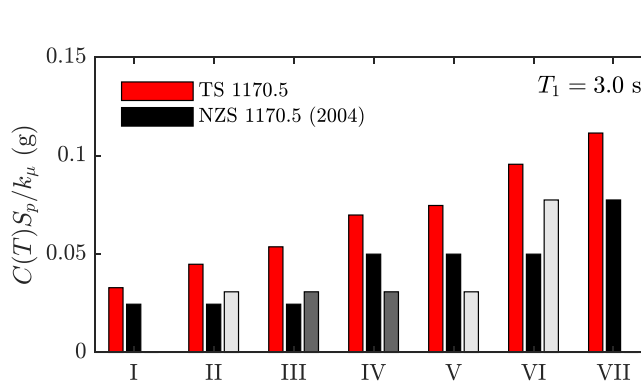
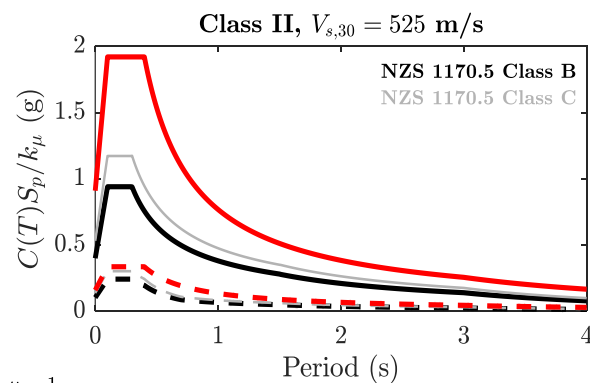
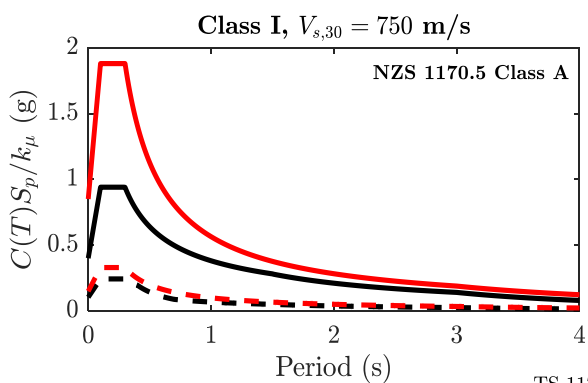
# WellingtonCBD, 500 years



**T = 0.2s**



**T = 1.0s**



**T = 3.0s**

- TS 1170.5,  $\mu = 1$
- NZS 1170.5 (2004),  $\mu = 1$
- - - TS 1170.5,  $\mu = 4, S_p = 0.7$
- - - NZS 1170.5(2004),  $\mu = 4, S_p = 0.7$

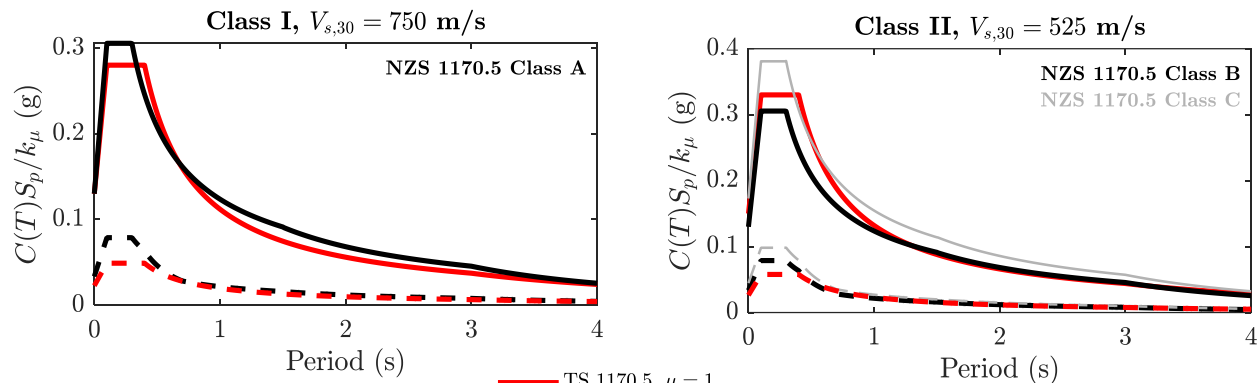
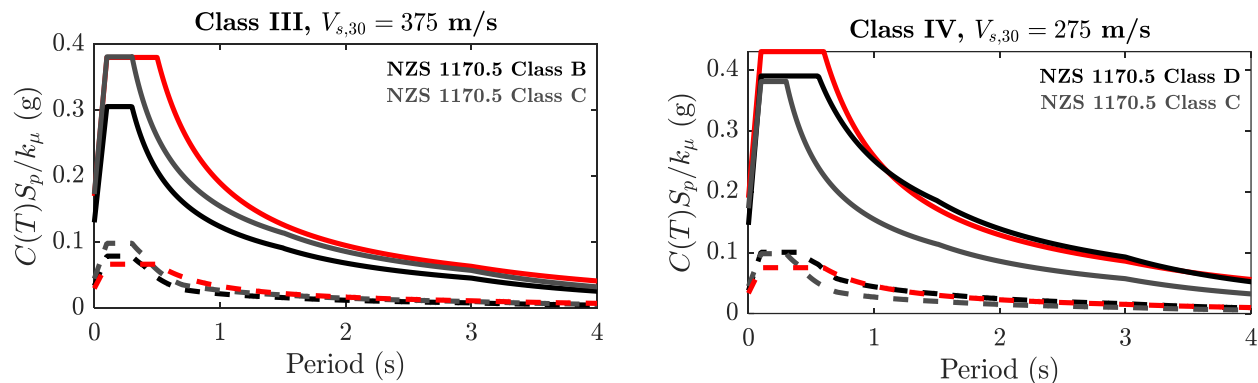
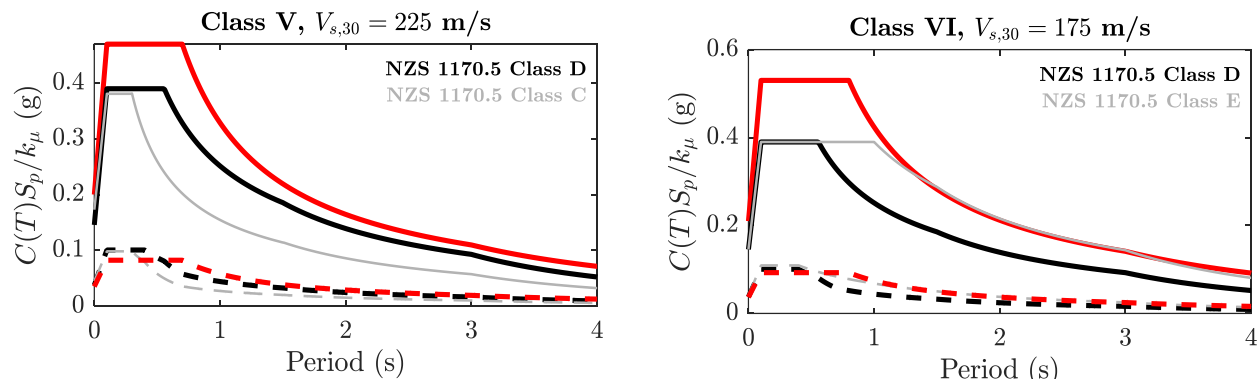
Light grey lines and text show less relevant soil class

Black and dark grey lines show equally relevant soil classes

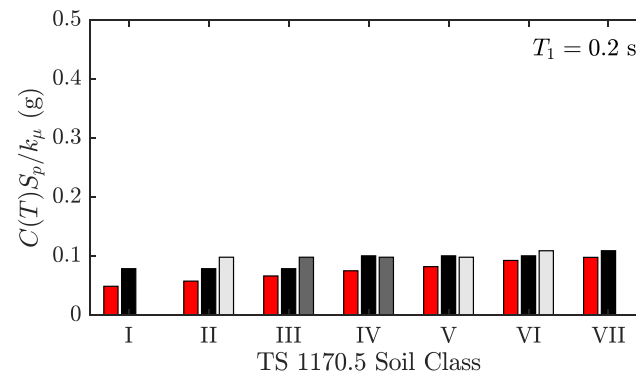
**ROCK**

**SOFT SOIL**

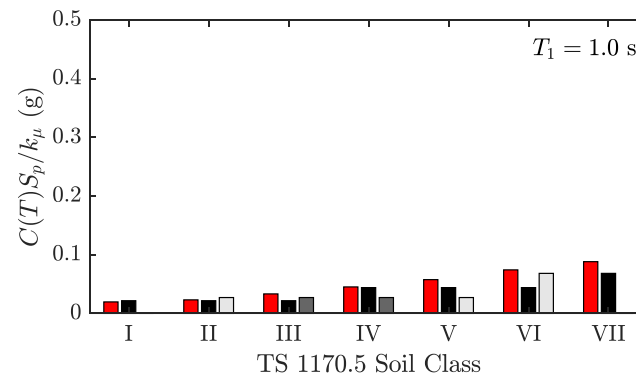
# Auckland, 500 years



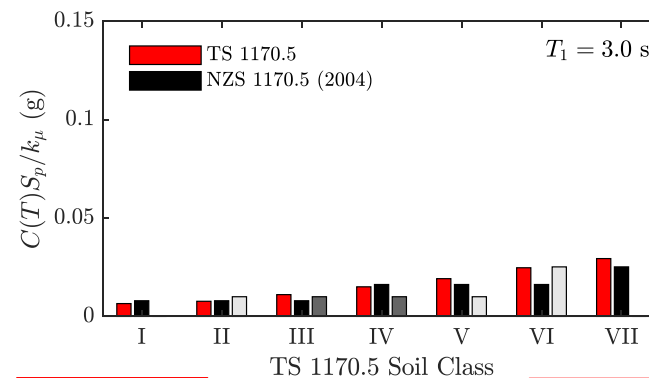
- TS 1170.5,  $\mu = 1$
- NZS 1170.5 (2004),  $\mu = 1$
- - - TS 1170.5,  $\mu = 4, S_p = 0.7$
- - - NZS 1170.5(2004),  $\mu = 4, S_p = 0.7$



**T = 0.2s**



**T = 1.0s**



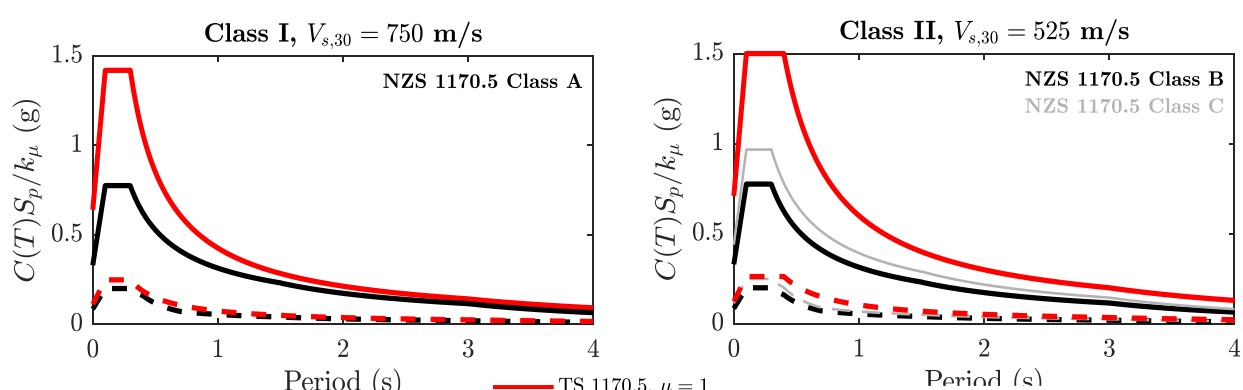
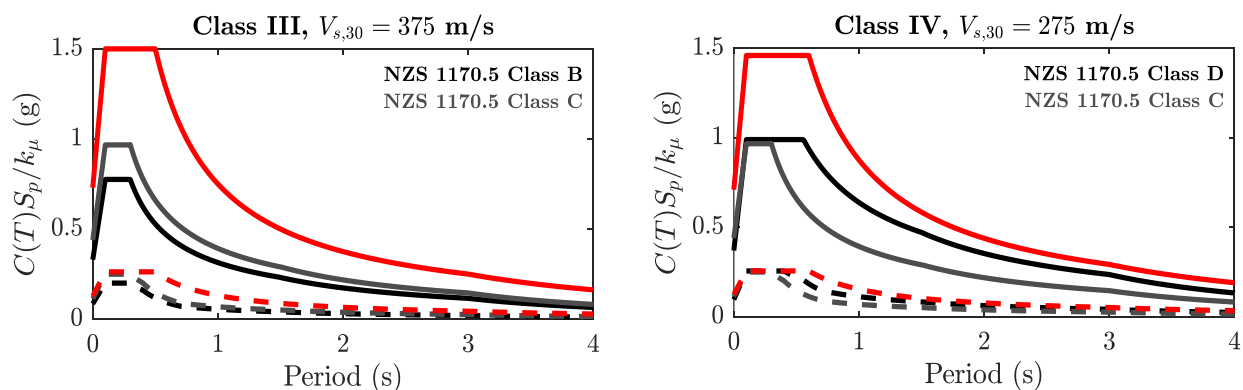
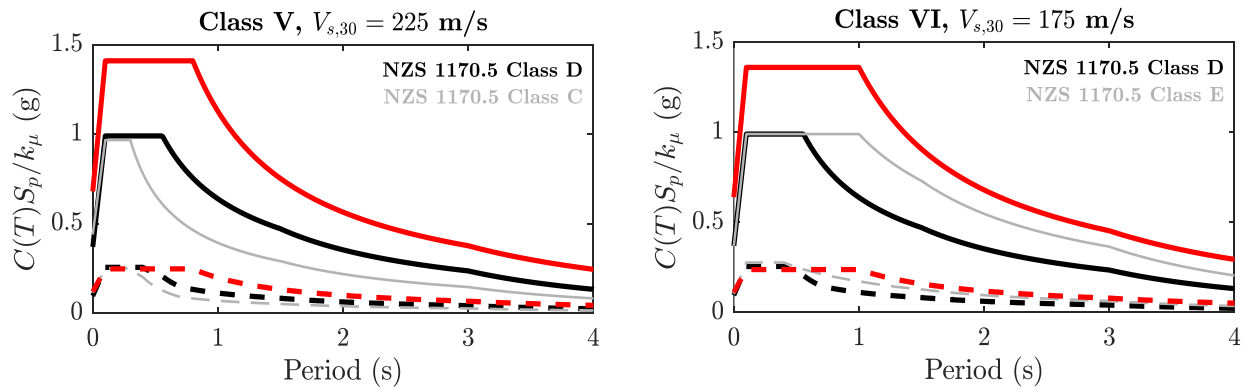
**T = 3.0s**

**ROCK**

**SOFT SOIL**

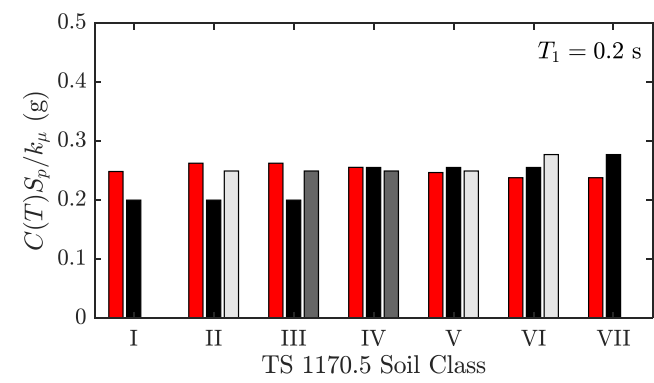


# Blenheim, 500 years

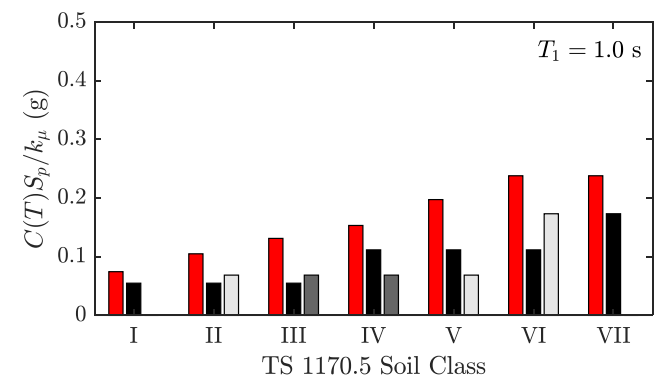


- TS 1170.5,  $\mu = 1$
- NZS 1170.5 (2004),  $\mu = 1$
- - - TS 1170.5,  $\mu = 4, S_p = 0.7$
- - - NZS 1170.5(2004),  $\mu = 4, S_p = 0.7$

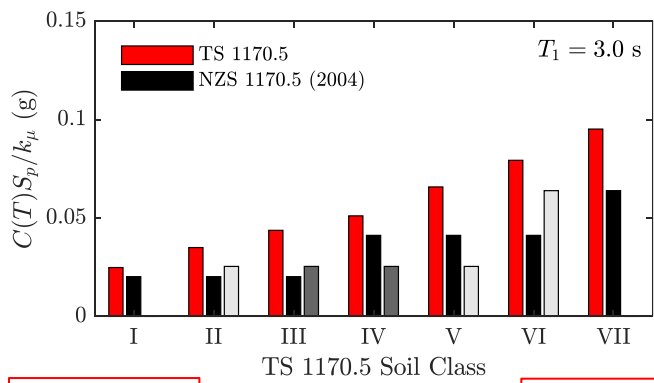
■ TS 1170.5  
■ NZS 1170.5 (2004)



$T = 0.2s$



$T = 1.0s$

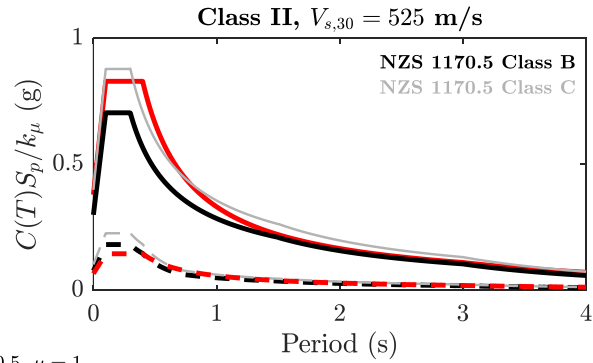
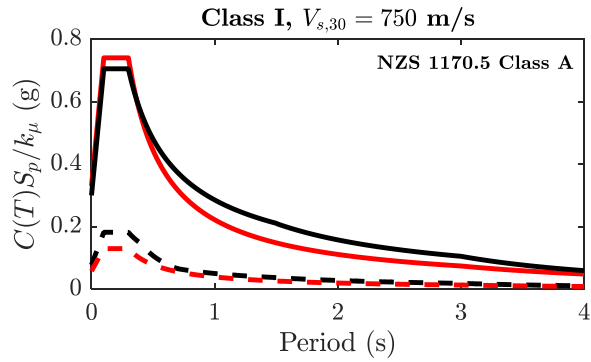
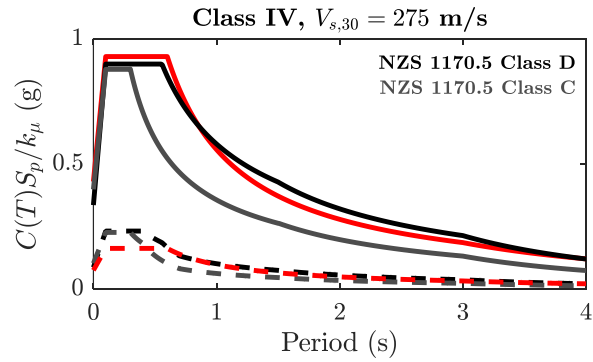
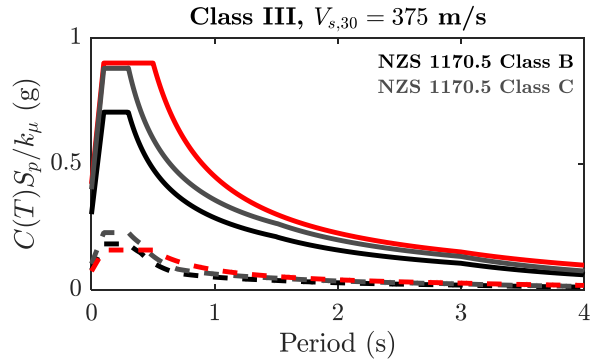
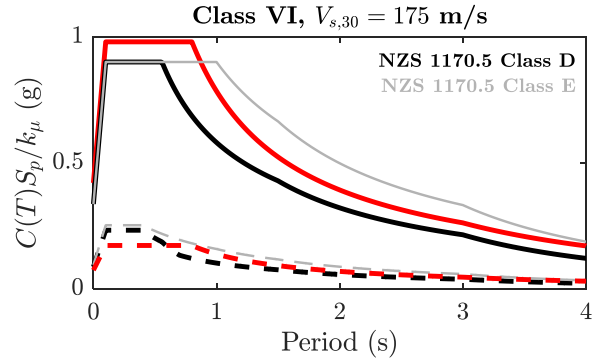
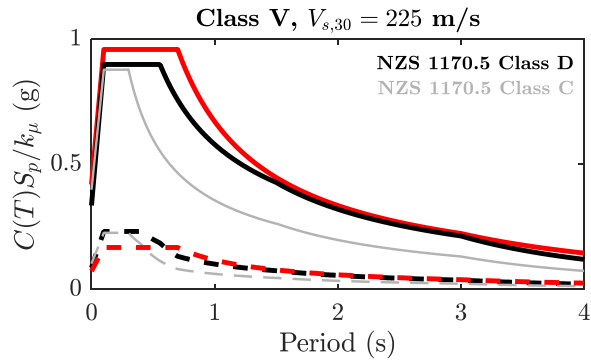


$T = 3.0s$

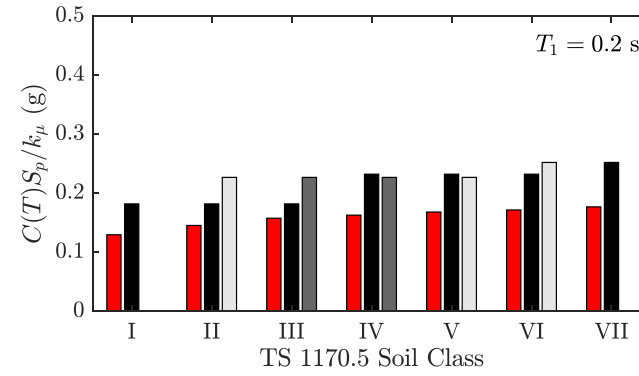
ROCK

SOFT SOIL

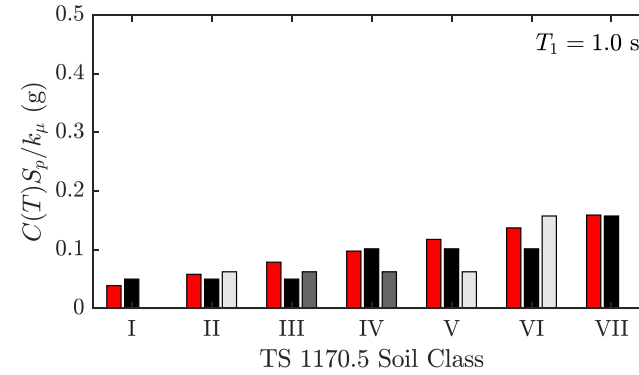
# Christchurch, 500 years



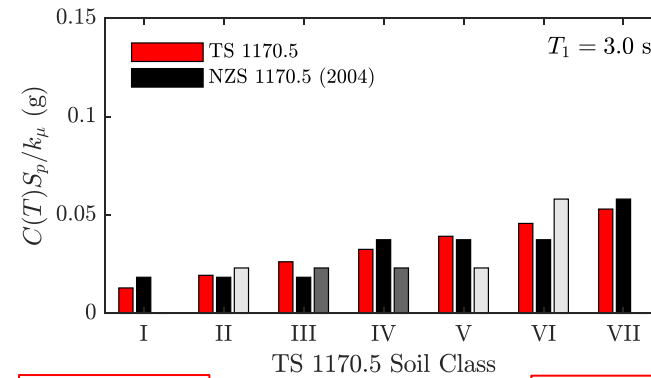
- TS 1170.5,  $\mu = 1$
- NZS 1170.5 (2004),  $\mu = 1$
- - - TS 1170.5,  $\mu = 4, S_p = 0.7$
- - - NZS 1170.5(2004),  $\mu = 4, S_p = 0.7$



**T = 0.2s**



**T = 1.0s**

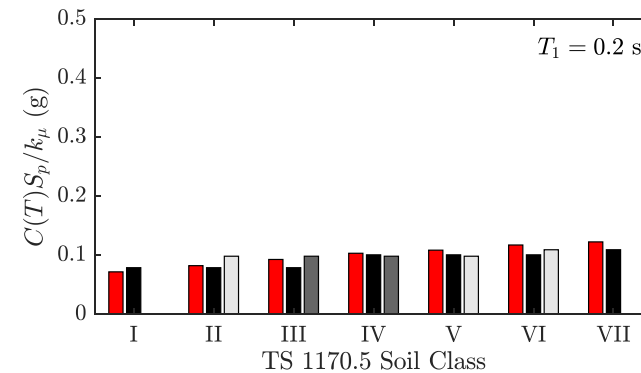
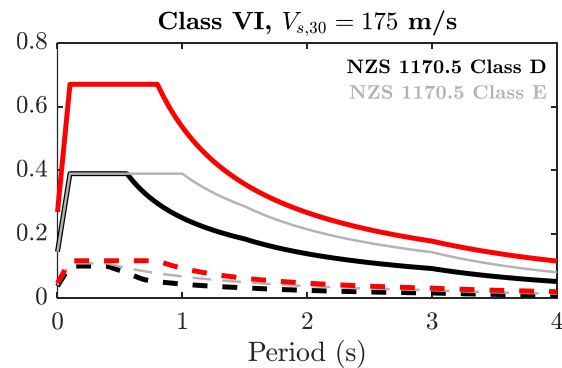
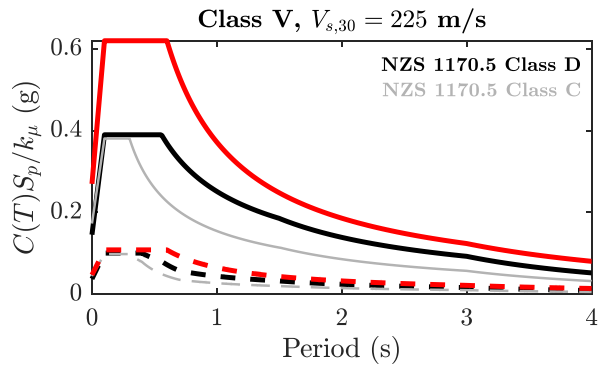
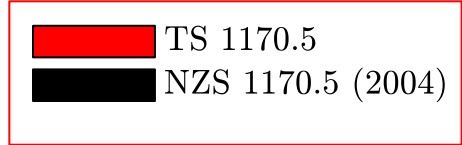


**T = 3.0s**

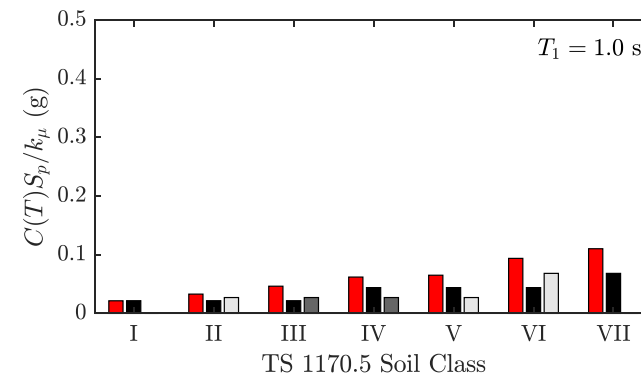
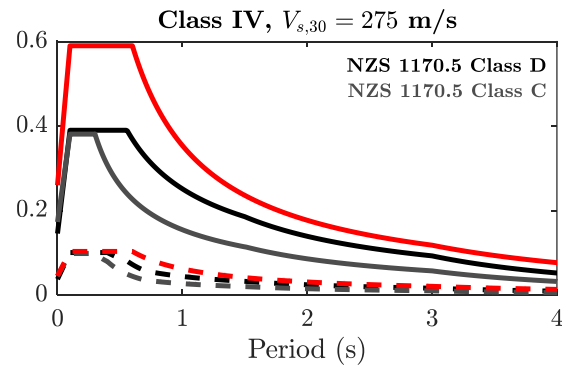
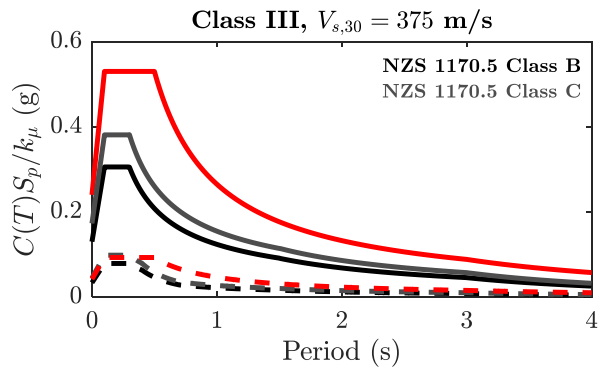
**ROCK**

**SOFT SOIL**

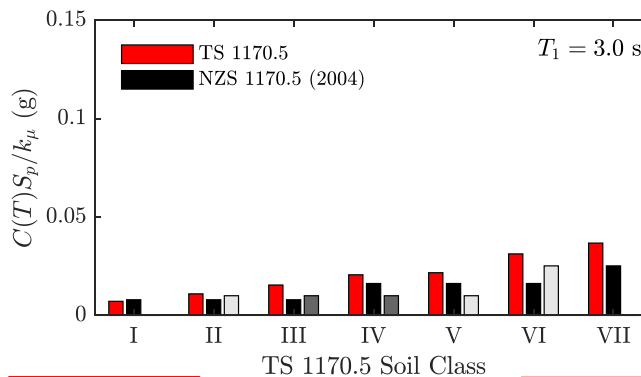
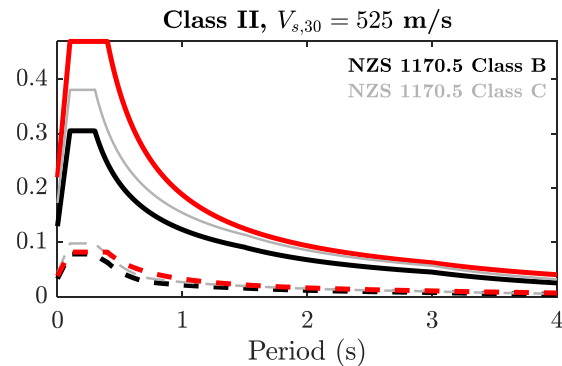
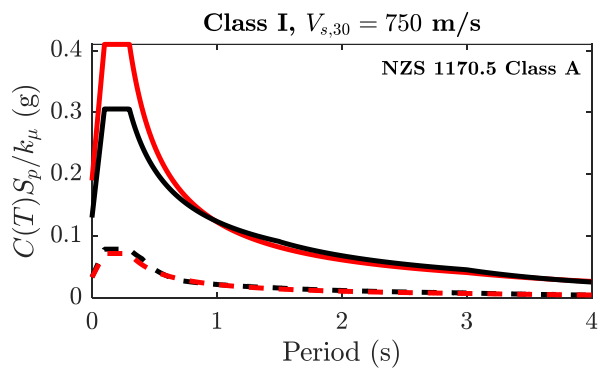
# Dunedin, 500 years



**T = 0.2s**



**T = 1.0s**



**T = 3.0s**

- TS 1170.5,  $\mu = 1$
- NZS 1170.5 (2004),  $\mu = 1$
- - - TS 1170.5,  $\mu = 4, S_p = 0.7$
- - - NZS 1170.5(2004),  $\mu = 4, S_p = 0.7$

**ROCK**

**SOFT SOIL**

Kia ora

Happy to answer questions at the end  
of today's webinar